

Accurate Modeling of InGaN QWs

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...translating ideas into innovation

Outline

- motivation
- theoretical model
- numerical results
 - TQW vs. SQW
(exp.: mostly TQW, theoret.: mostly SQW, no direct comparison)
 - influence of polarization fields and doping (screening)

Motivation

- wurtzite InGaN quantum wells – active region of violet, blue and green light emitting diodes and laser diodes
- spontaneous and piezoelectric polarisation fields \Rightarrow self-consistent solution of Poisson and Schrödinger equations necessary for computation of luminescence and gain spectra
- several shortcomings of published models
 - parabolic band approximation
 - only fundamental electron and hole states taken into account
 - excess carrier density acts as input parameter
 - boundary conditions for electro-static or Hartree potential and chemical potentials remain unclear

Energy bands and wave functions

Schrödinger equation: $8 \times 8 \mathbf{k} \cdot \mathbf{p}$ Hamiltonian taking into account 3 uppermost valence bands and lowest conduction band, doubly degenerated

$$\mathbf{H}\left(E_c^*, E_v^*, \mathbf{k}_{||}, \frac{d}{dz},\right) \Psi_n(\mathbf{k}_{||}, z) = E_n(\mathbf{k}_{||}) \Psi_n(\mathbf{k}_{||}, z)$$

renormalization of bulk band edges

$$E_c^* = E_c - e\phi_H - \frac{1}{2}V_{xc}\left(\frac{n+p}{2}\right)$$

$$E_v^* = E_v - e\phi_H + \frac{1}{2}V_{xc}\left(\frac{n+p}{2}\right)$$

V_{xc} exchange–correlation potential in local density approximation

ϕ_H Hartree potential from Maxwell's equation

Hartree potential

Poisson equation

$$\operatorname{div} \mathbf{D} = e(p - n + N_{\text{D}}^+ - N_{\text{A}}^-) - \operatorname{div} \mathbf{P}$$

$$\mathbf{D} = -\epsilon_0 \epsilon_r \operatorname{grad} \phi_H$$

electron and hole densities

$$n = n^{2D} + n^{3D}, \quad p = p^{2D} + p^{3D}$$

quantum electron density

$$n^{2D} = \sum_{n_c} \frac{1}{4\pi^2} \int |\Psi_{n_c}(\mathbf{k}_{||})|^2 f\left(\frac{E_{n_c}(\mathbf{k}_{||}) - e\phi_n}{k_B T}\right) d^2 \mathbf{k}_{||}$$

free electron density

$$n^{3D} = N_c F_{1/2} \left(\frac{\max(E_{n_c}(0), E_c^*) - e\phi_n}{k_B T} \right)$$

similar for p^{2D} and p^{3D}

macroscopic polarization

$$\mathbf{P} = \mathbf{P}_{\text{spont}} + \mathbf{P}_{\text{piezo}}$$

Boundary conditions

- wavefunction

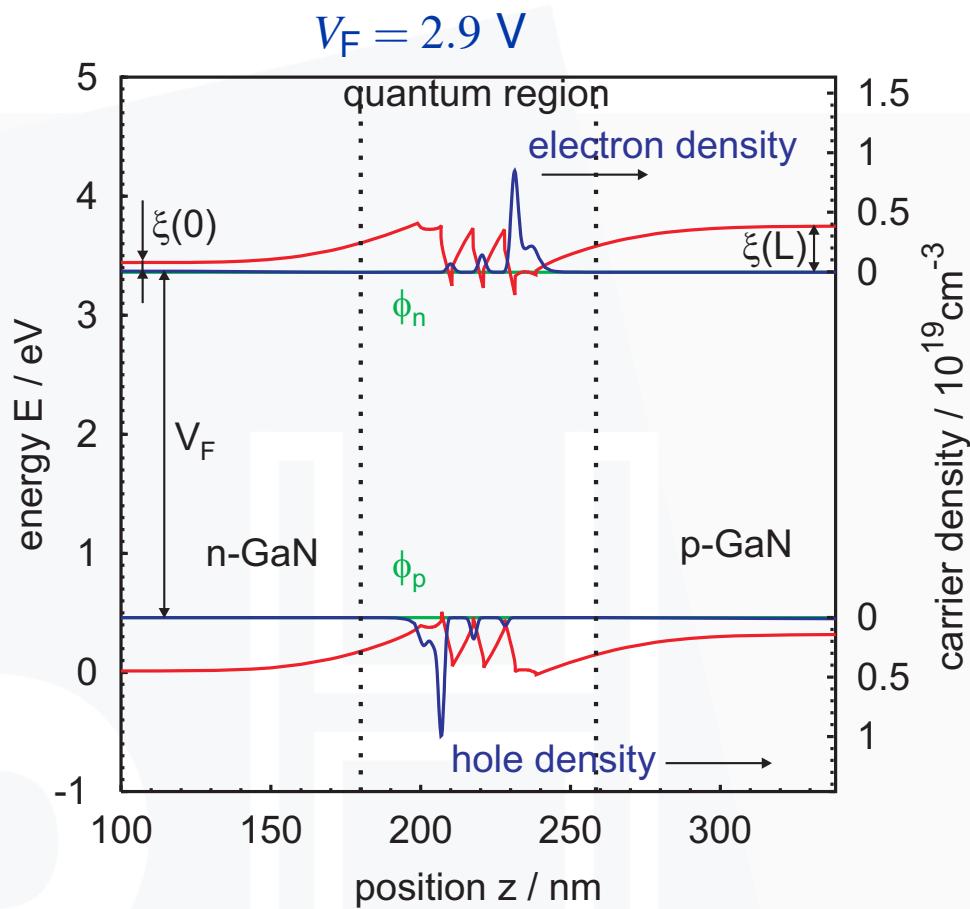
$$\Psi_n = 0$$

at boundaries of quantum region

- Hartree potential

$$\phi_H(0) = 0$$

$$\phi_H(L) = \xi(L) - \xi(0)$$



chemical potentials ξ solutions of bulk neutrality condition at $z = 0, L$

$$N_v F_{1/2} \left(\frac{eV_F - E_g - e\xi}{k_B T} \right) - N_c F_{1/2} \left(\frac{e\xi}{k_B T} \right) + N_D^+ - N_A^- = 0$$

input parameter $V_F = \phi_n - \phi_p$ Fermi voltage

Numerics

- Schrödinger equation: Galerkin method (sinus functions) \Rightarrow algebraic eigenvalue problem solved with LAPACK routine ZHEEV
- nonlinear Poisson equation: discretized with finite differences, solved with Newton's method
- iteration using implicit scheme where subband energies E_{n_c} are replaced by $E_{n_c} - (\phi_H^k(z) - \phi_H^{k-1}(z))$ in expression for n^{2D} (similarly for p^{2D}) \Rightarrow faster convergence
- luminescence and gain: free carrier theory with sech-type of broadening (FWHM 26 meV)
- $T = 300$ K in all simulations

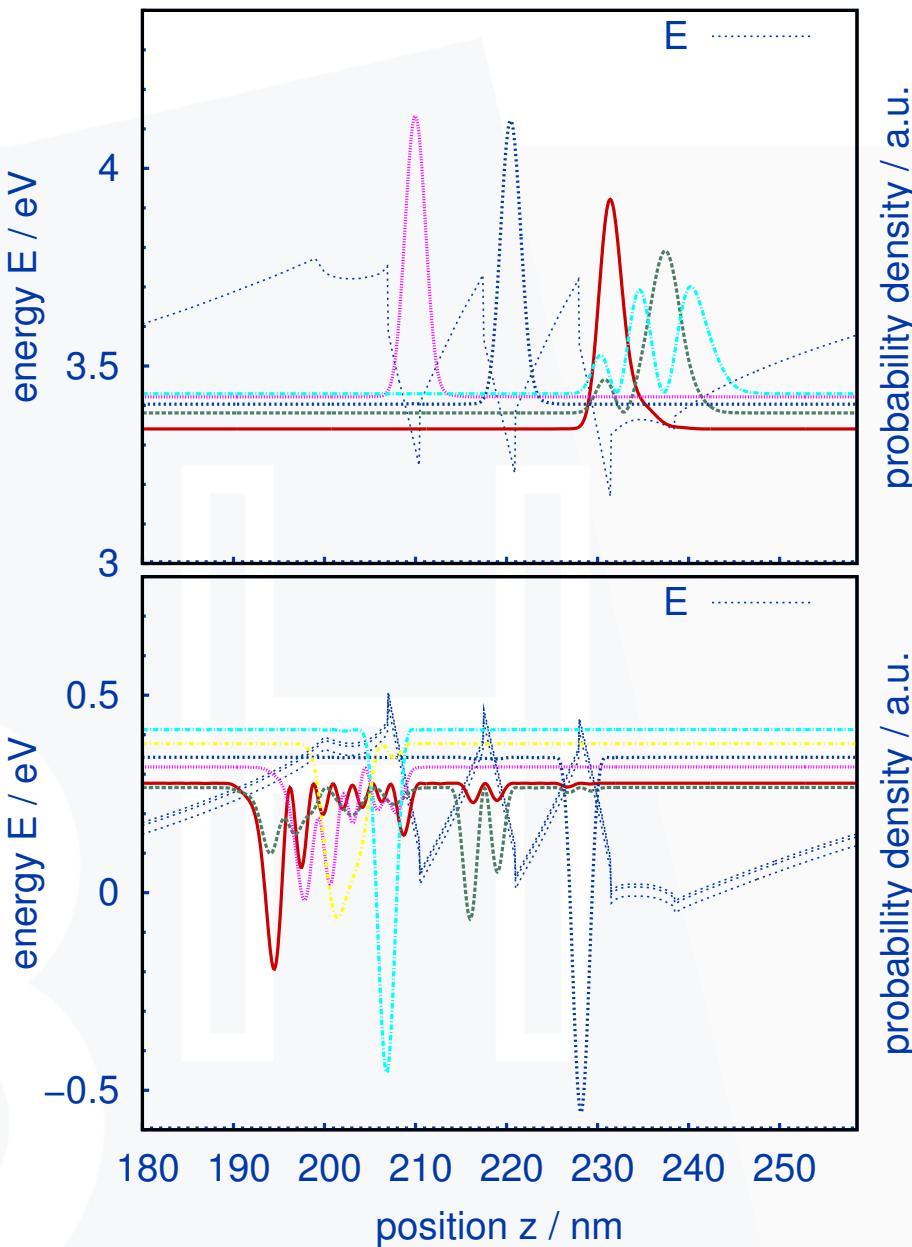
Structure

| layer | compound | d nm | D cm^{-3} | $P_{\text{spont},z}$ $10^{-6} \text{ C cm}^{-2}$ | $P_{\text{piezo},z}$ $10^{-6} \text{ C cm}^{-2}$ |
|-------------|--|-----------|-------------------------|---|---|
| confinement | n-GaN | 200 | $+10^{17}$ | -3.40 | 0 |
| barrier | $\text{In}_{0.015}\text{Ga}_{0.985}\text{N}$ | 7 | $+10^{16}$ | -3.36 | +0.22 |
| QW | $\text{In}_{0.09}\text{Ga}_{0.91}\text{N}$ | 3.5 | $+10^{16}$ | -3.17 | +1.42 |
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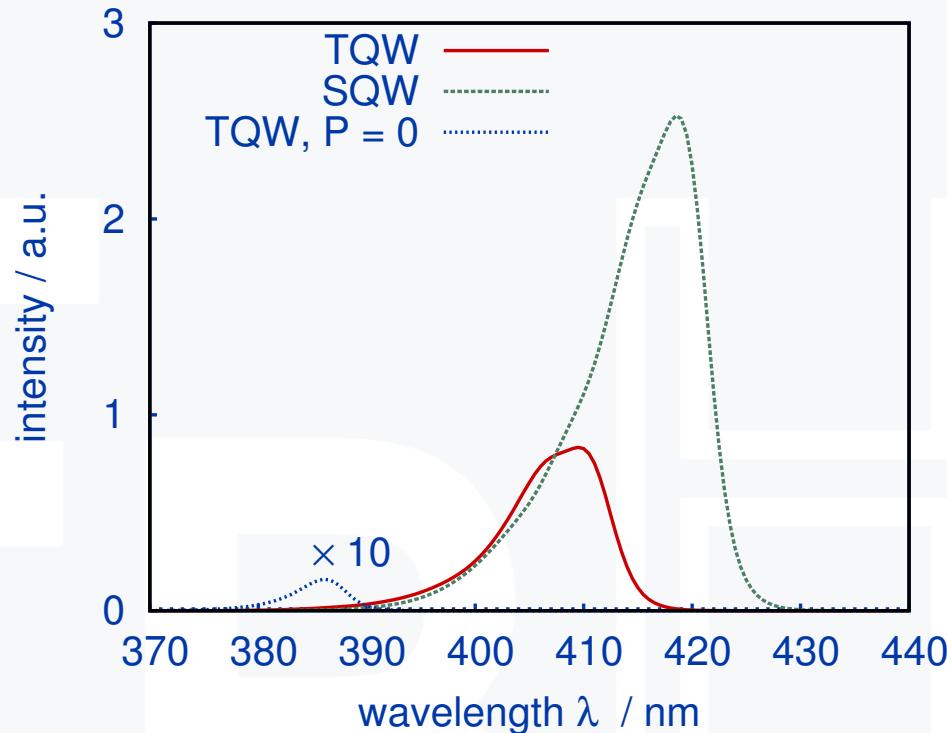
Quantum region

conduction and valence band edges, probability densities

- first electron (hole) states are located in first (last) QW and left (right) barrier
- poor spatial overlap of highly occupied states
- states with better overlap less occupied

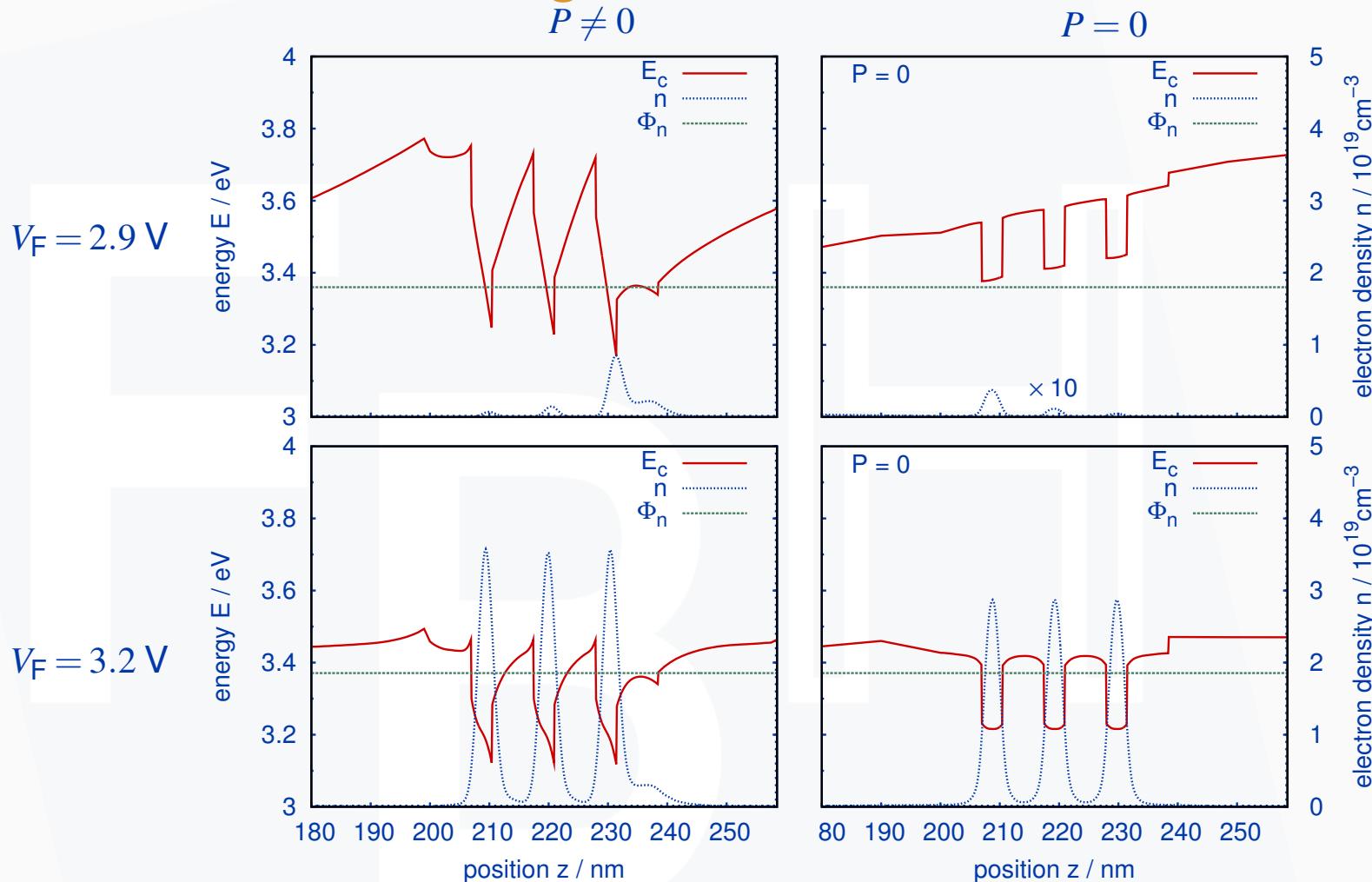


Luminescence spectra $V_F = 2.9$ V

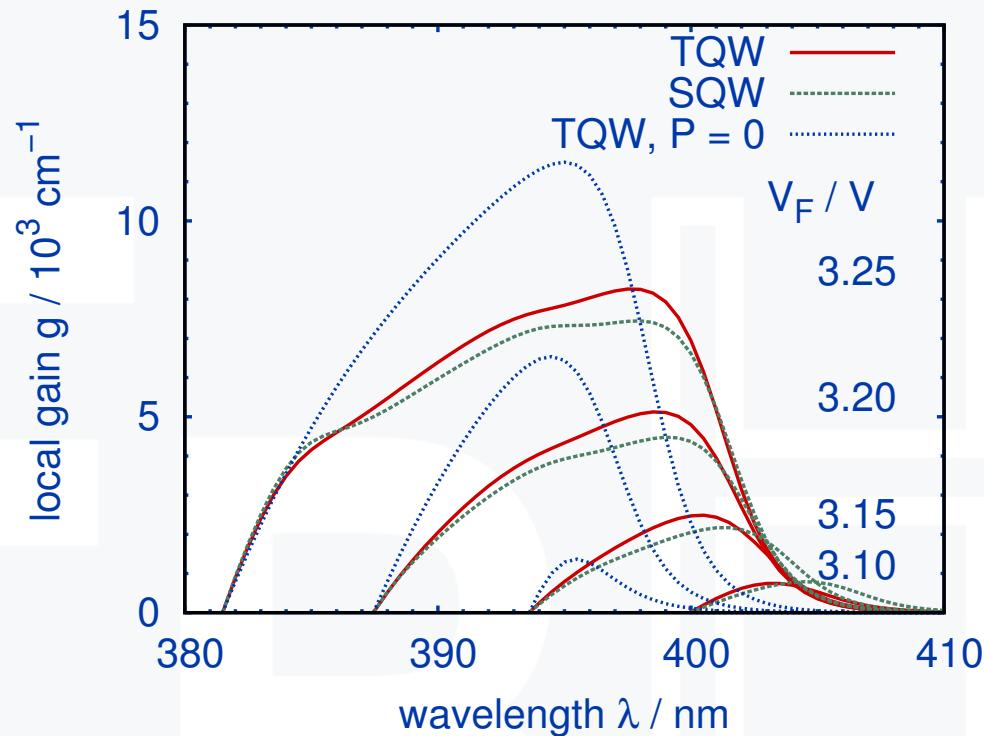


- luminescence peak of SQW red-shifted and larger due to larger spatial overlap of highly occupied states
- luminescence of TQW for vanishing polarization 2 orders of magnitude smaller

Conduction band edges and electron densities



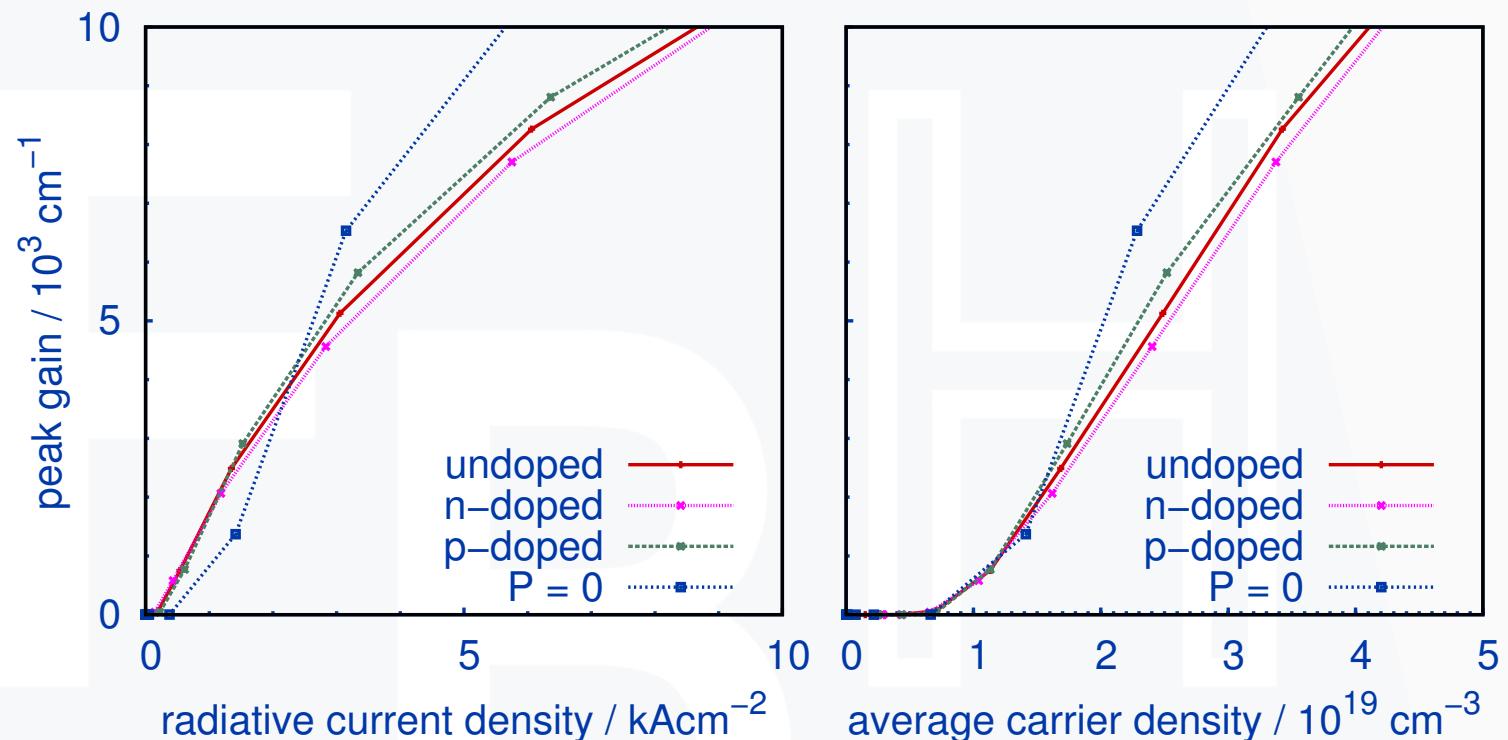
Gain spectra



- gain with full polarization fields enhanced at smaller bias, reduced at larger bias, blue-shifted compared to the case of $P = 0$
- almost no difference in gain spectra between SQW and TQW

Impact of doping of barriers on gain peak of TQW

n-doping: $N_D^+ = 5 \times 10^{18}$, p-doping: $N_A^- = 5 \times 10^{18}$



almost no difference in gain peak dependence on radiative current density or on carrier density between undoped and doped barriers

Summary

- self-consistent solution of the Poisson equation and an eight-band $k \cdot p$ Schrödinger equation for wurtzite strained InGaN quantum wells taking into account proper boundary conditions for the Hartree and chemical potentials
- application to SQW and TQW structures embedded in a p-n junction
- stronger and red-shifted luminescence of SQW compared to TQW for the same Fermi voltage (bias)
- enhancement of luminescence and gain at lower bias due to polarisation fields
- almost identical gain spectra of SQW and TQW structures
- only minor impact of doping of barriers on gain