
Nested Ring Mach-Zehnder Interferometer (NRMZI)

Photonics Research Centre
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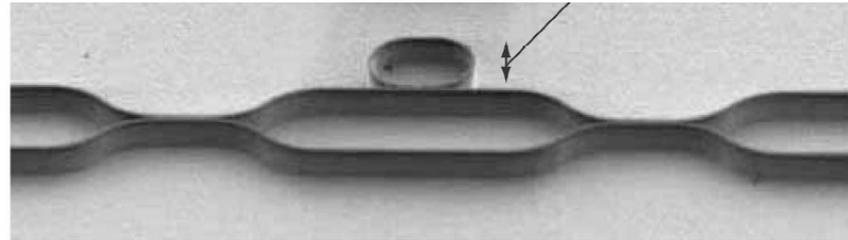
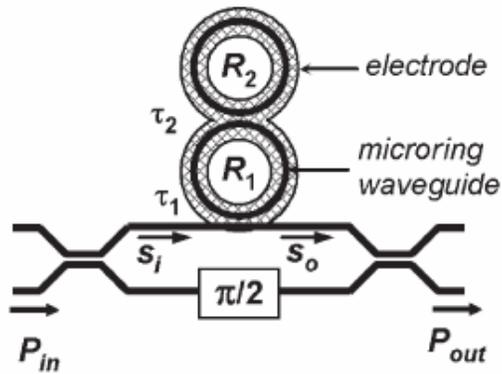
Presented by: Stevanus Darmawan and M. K. Chin

*Special thanks to Landobasa Y. M. for fruitful discussions

Outline

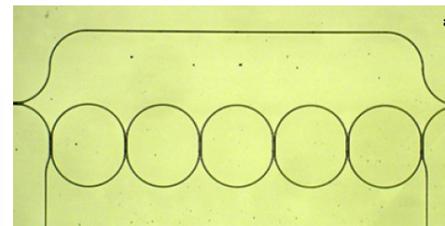
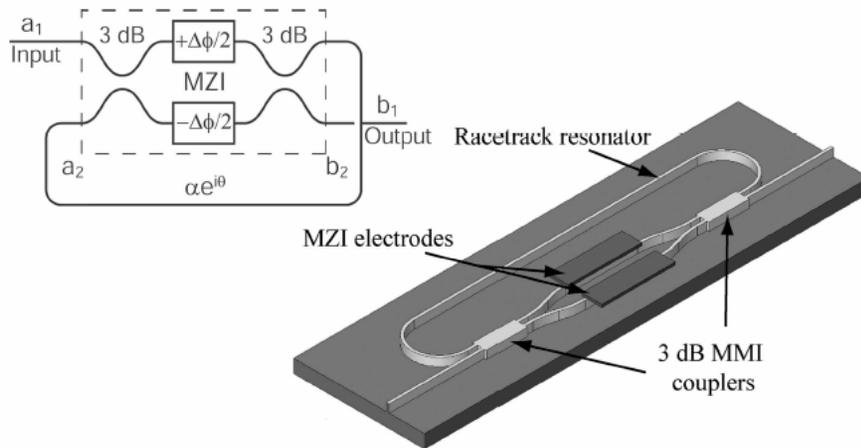
- Introduction: Some literature review
- Motivation: Why NRMZI?
- Theory: Device modeling
- Results: Box-like output and ultra-sharp resonance
- Conclusion

Literature on RR + MZIs



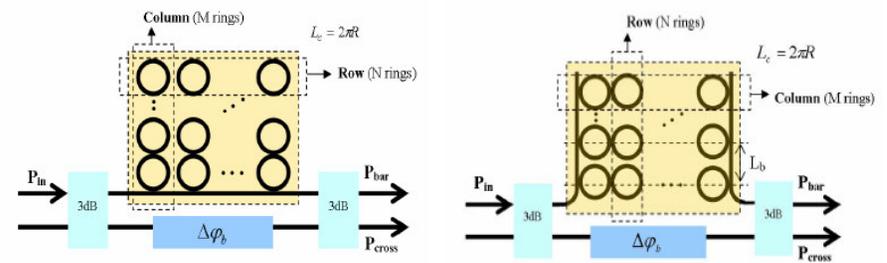
Ring enhanced Mach-Zehnder interferometer (**REMZI**)
J. E. Heebner, et al ; Y. Lu, et al

Linearized micro-ring loaded MZI
V. Van et al



Serially coupled REMZI
George T. Paloczi et al

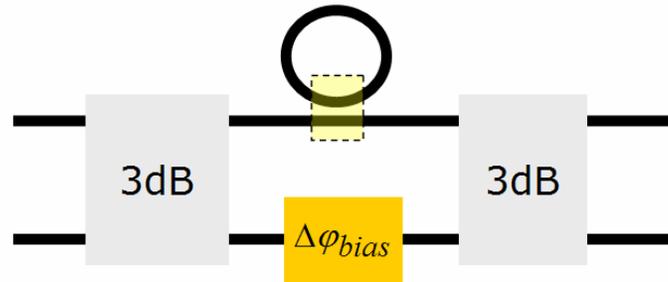
Ring feedback Mach-Zehnder interferometer (**RFMZI**)
C.Y. Chao and L. J. Guo
William M. J. Green et al



Ring arrays - MZI
S. Darmawan et al

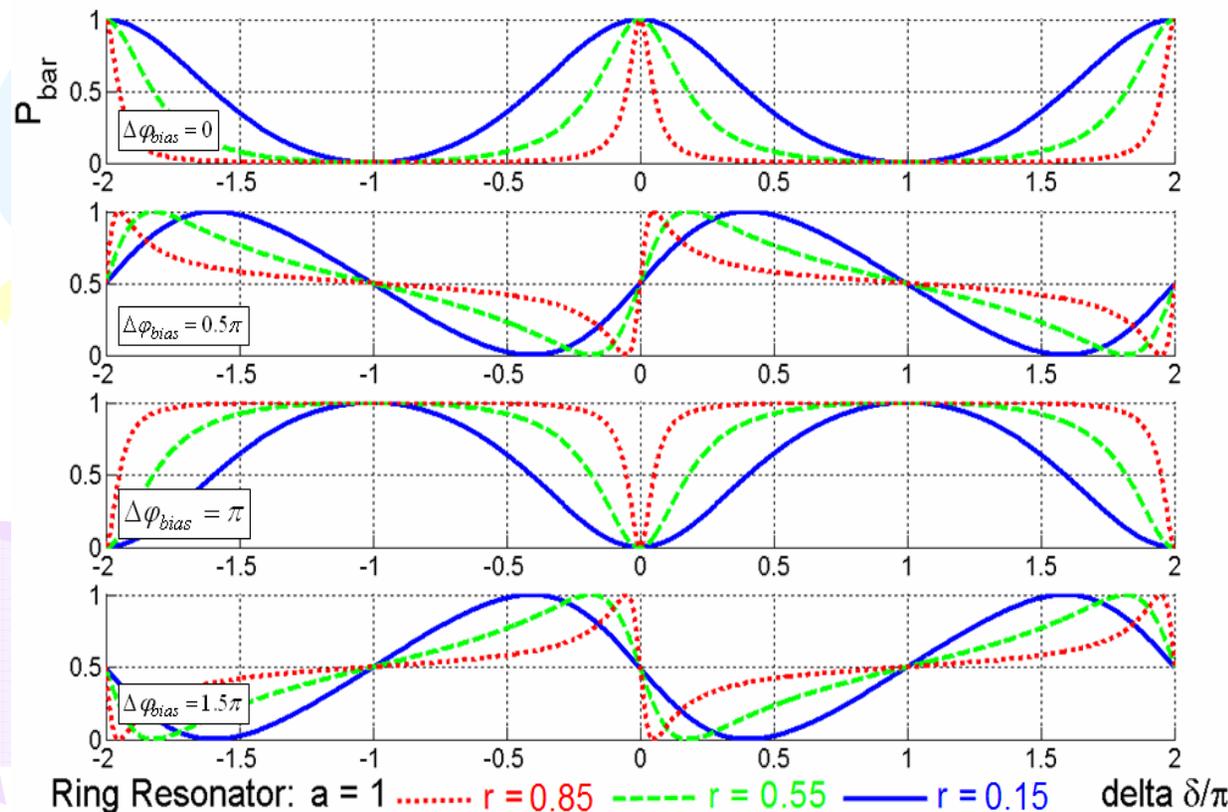
Why REMZI ?

Ring enhanced Mach-Zehnder interferometer (**REMZI**)
J. E. Heebner, et al ; Y. Lu, et al



$$P_{bar} = \sin^2 [(\varphi_{ring} - \Delta\varphi_{bias}) / 2]$$

$$P_{cross} = \cos^2 [(\varphi_{ring} - \Delta\varphi_{bias}) / 2]$$

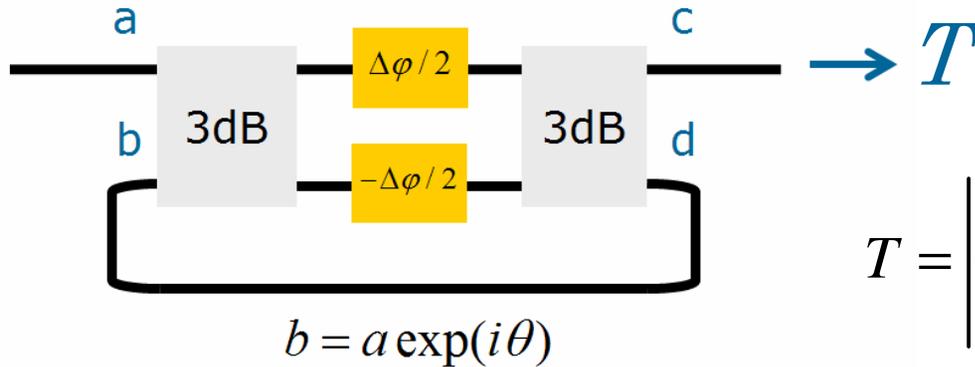


May function as:

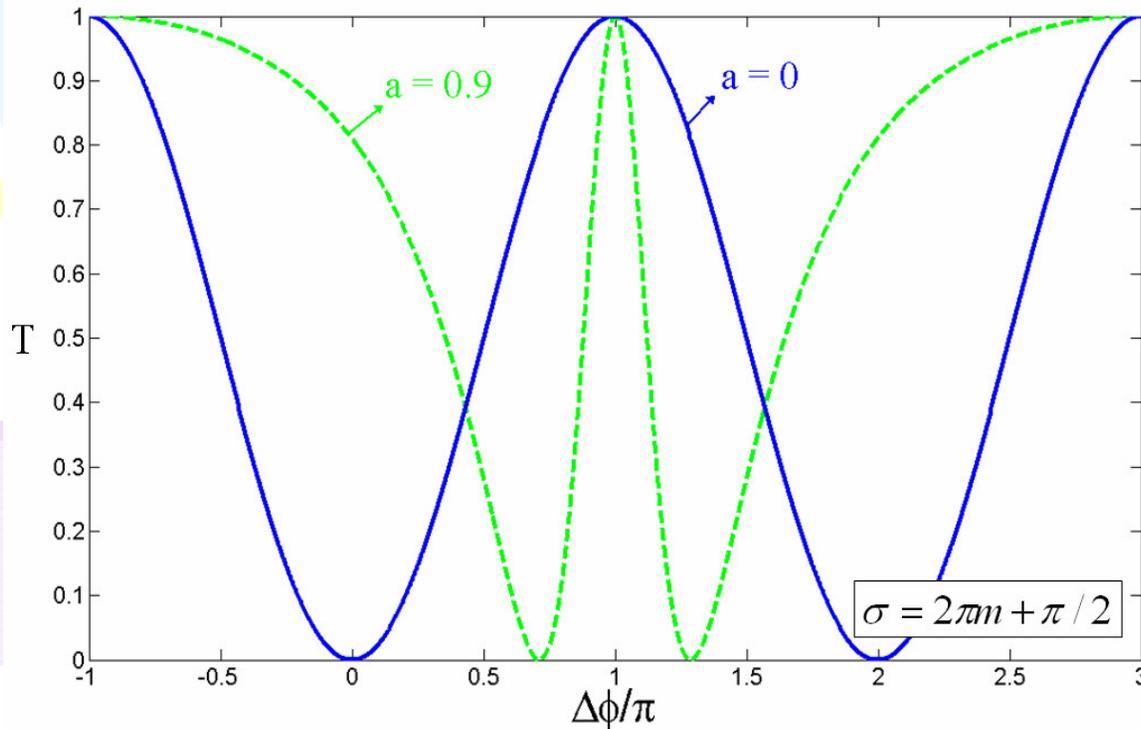
- Modulator
- Switches
- Sensors

$$\delta = 2\pi n_{eff} L_c / \lambda$$

Why RFMZI ?



$$T = \left| \frac{i \sin(\Delta\phi/2) - a \exp(i\sigma)}{1 + ia \sin(\Delta\phi/2) \exp(i\sigma)} \right|^2$$



May function as:

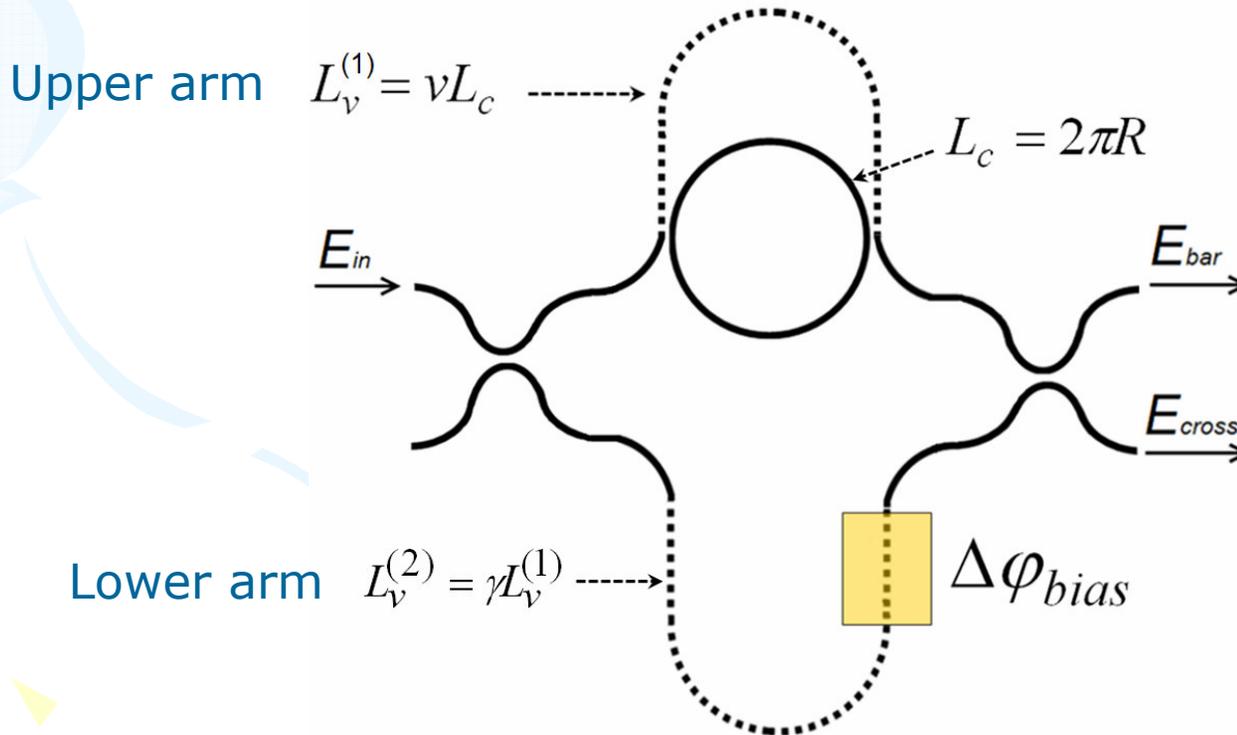
- Modulator
- Switches
- Sensors

Ring feedback Mach-Zehnder
interferometer (**RFMZI**)
C.Y. Chao and L. J. Guo
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Motivation: Why NRMZI ?

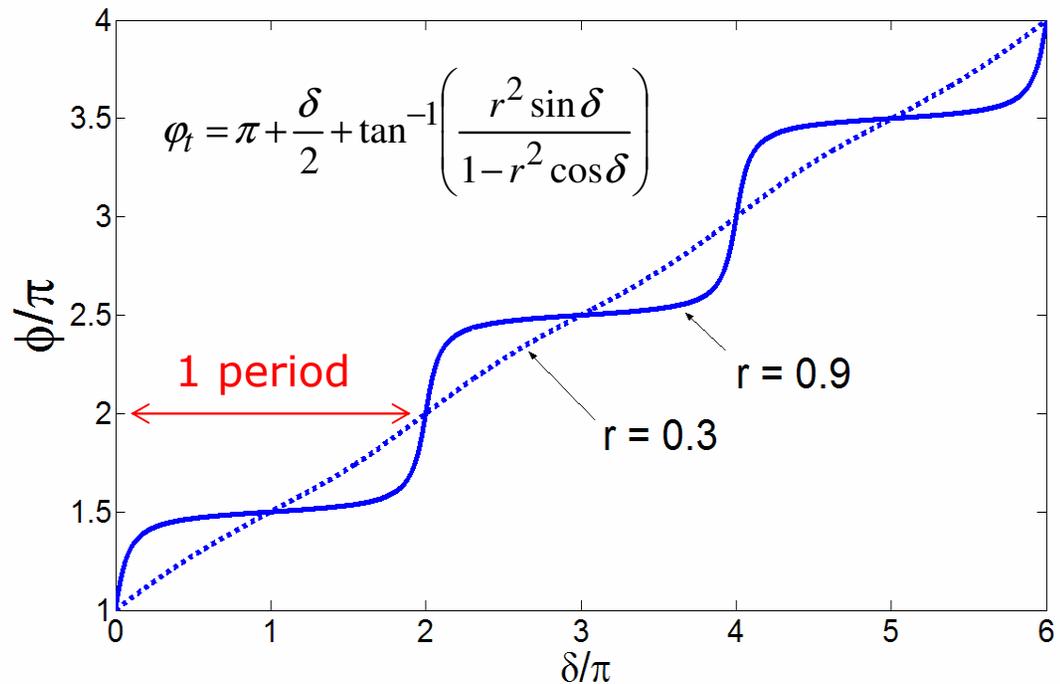
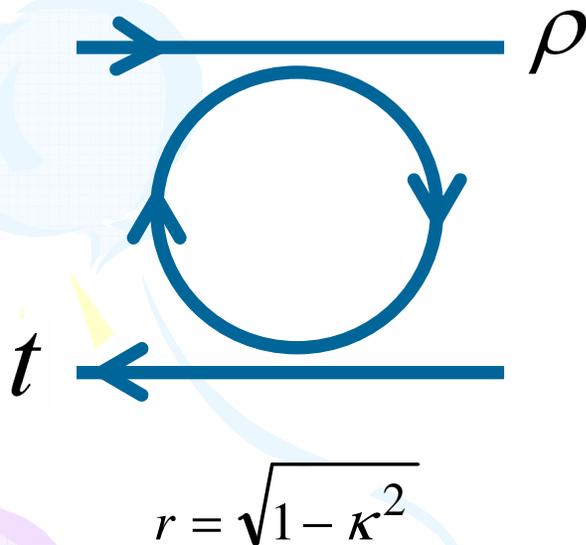
Feature of interest:

- Good linearity with lower pumping power (as Modulator)
- Ultra-sharp resonance (as Sensor)
- Produces a box-like spectrum (as Filter)



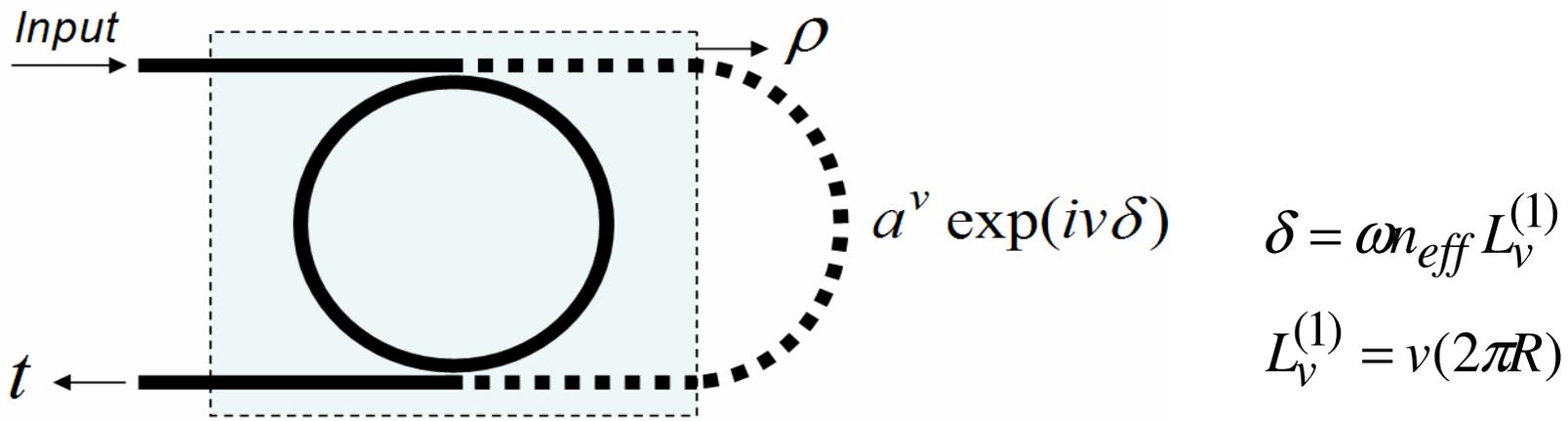
Basic: Dual-bus RR

$$\rho = \frac{r[-1 + a \exp(i\delta)]}{1 - r^2 a \exp(i\delta)} \quad t = \frac{-\kappa^2 \sqrt{a} \exp(i\delta/2)}{1 - r^2 a \exp(i\delta)}$$



Build up factor $B = \frac{\partial \varphi}{\partial \delta}$ is high when (r) is high

Loaded Nested RR (NRR)



Based on the topology of a dual-bus ring with closed loop feedback:

$$\begin{aligned}
 t_{ring} &= t + \rho^2 a^v \exp(iv\delta) [1 + ta^v \exp(iv\delta) + \dots] \\
 &= t + \frac{\rho^2 a^v \exp(iv\delta)}{1 - ta^v \exp(iv\delta)} = \frac{t + (\rho^2 - t^2) a^v \exp(iv\delta)}{1 - ta^v \exp(iv\delta)}
 \end{aligned}$$

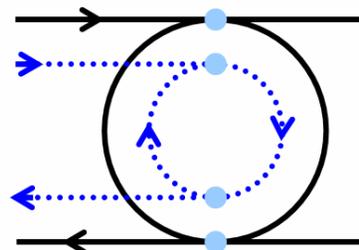
Phase response of NRR

For a lossless case, the loaded phase response of NRR can be expressed as:

$$\varphi_{NRR}^{loaded} = \varphi_t + \varphi_{loading} =$$

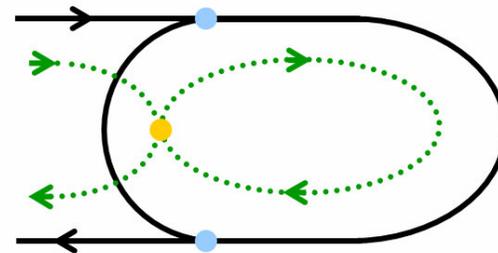
$$\varphi_t - \tan^{-1} \left(\frac{\sin(v\delta + \varphi_t)}{|t| - \cos(v\delta + \varphi_t)} \right) + \tan^{-1} \left(\frac{|t| \sin(v\delta + \varphi_t)}{1 - |t| \cos(v\delta + \varphi_t)} \right)$$

$$\varphi_t = \pi + \frac{\delta}{2} + \tan^{-1} \left(\frac{r^2 \sin \delta}{1 - r^2 \cos \delta} \right)$$



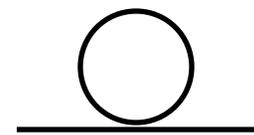
φ_t Dual-bus RR

$$\varphi = -\tan^{-1} \left(\frac{\sin \delta}{r - \cos \delta} \right) + \tan^{-1} \left(\frac{r \sin \delta}{1 - r \cos \delta} \right)$$



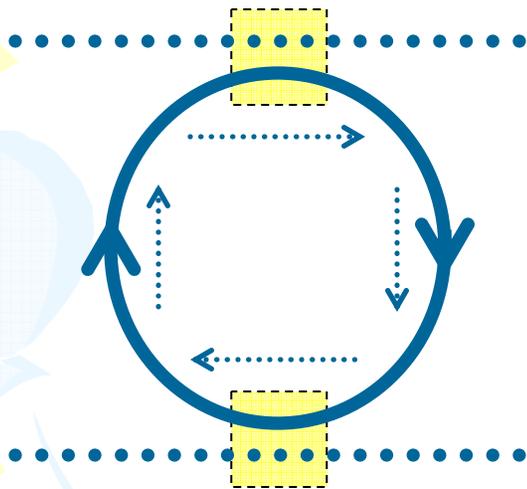
$\varphi_{loading}$

Single-bus RR



Two 'competing' resonant loops

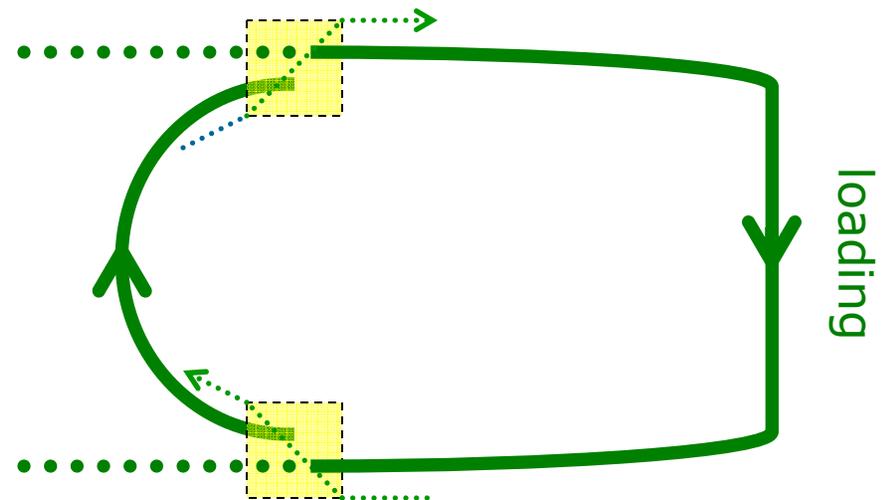
Inner resonant loop



$$r = \sqrt{1 - \kappa^2}$$

'Reflection' based resonance

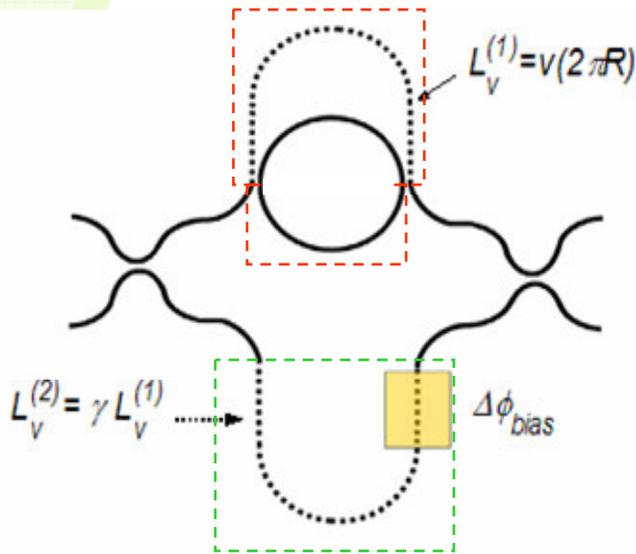
Outer resonant loop



$$\kappa = \sqrt{1 - r^2}$$

'Coupling' based resonance

Engineering a box-like transmission

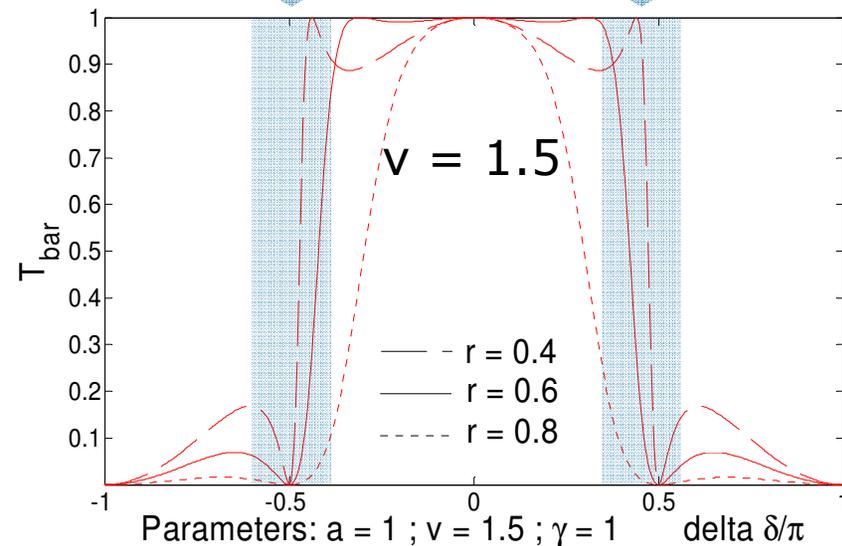
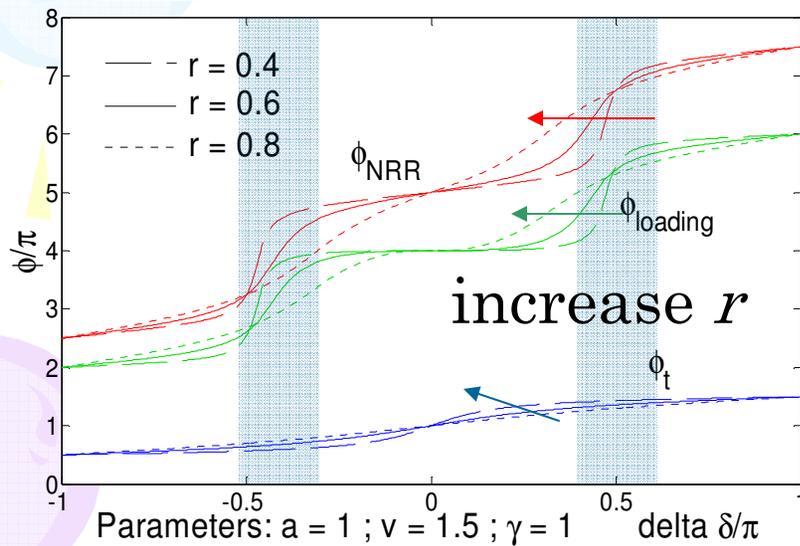


By optimizing (v) and (r) values !

$$T_{bar} = \sin^2([\varphi_{NRR} - (\mathcal{W}\delta + \Delta\varphi_{bias})]/2)$$

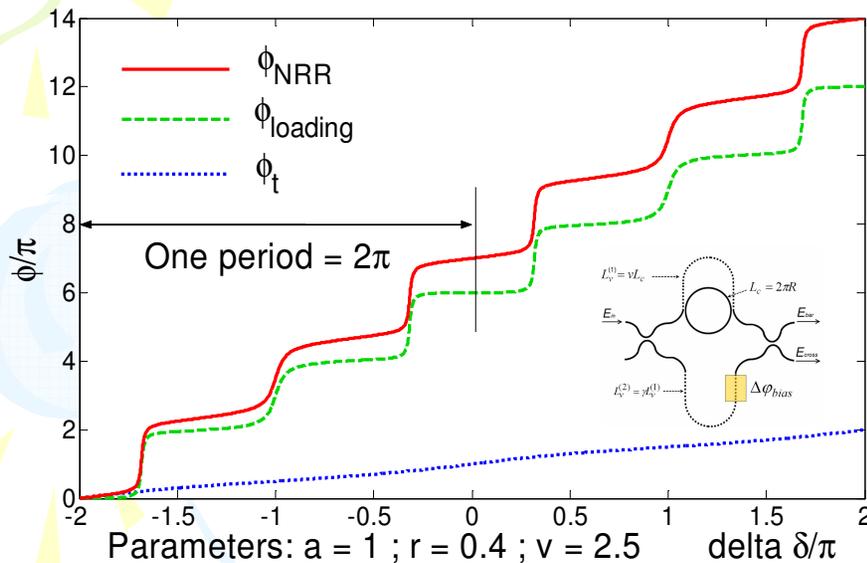
$$T_{cross} = \cos^2([\varphi_{NRR} - (\mathcal{W}\delta + \Delta\varphi_{bias})]/2)$$

Double-Fano resonance

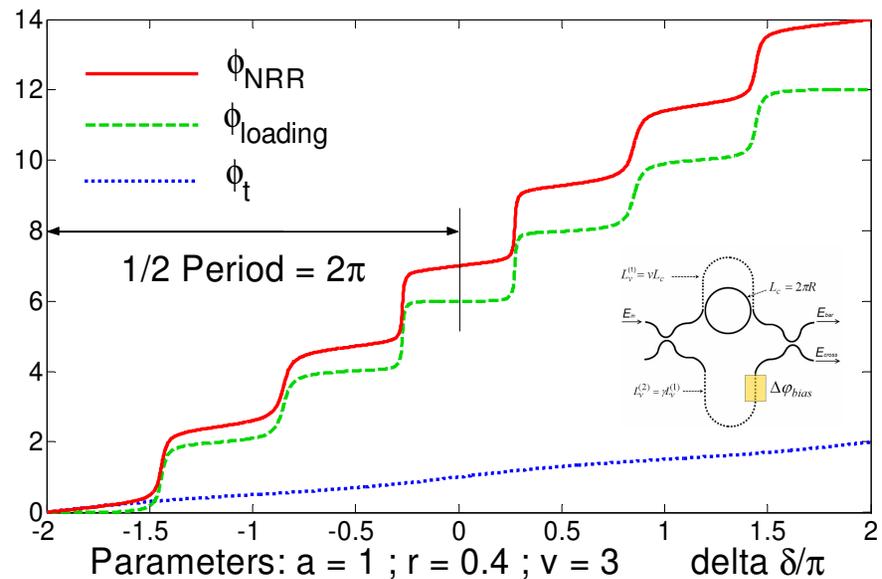


Conditions of ν for box-like transmission

- Box-like only at: $\nu = m-1/2 \rightarrow 2\pi$ period and $\nu = m \rightarrow 4\pi$ period



$(\nu = m-1/2)$



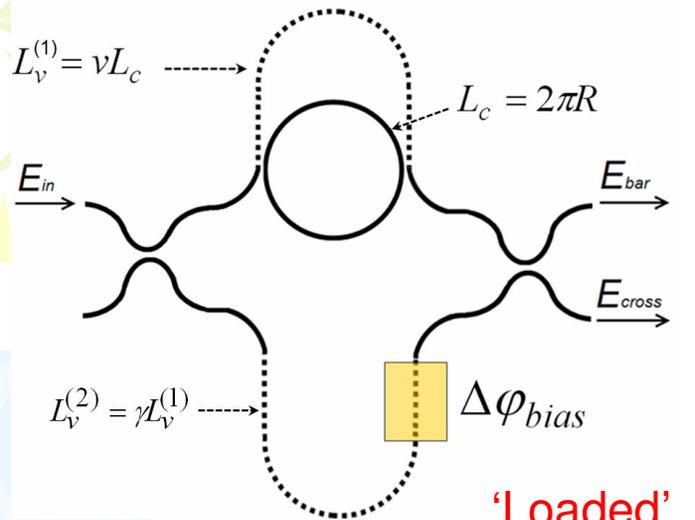
$(\nu = m)$

$$\text{loaded } \phi_{NRR} = \phi_t + \phi_{\text{loading}} =$$

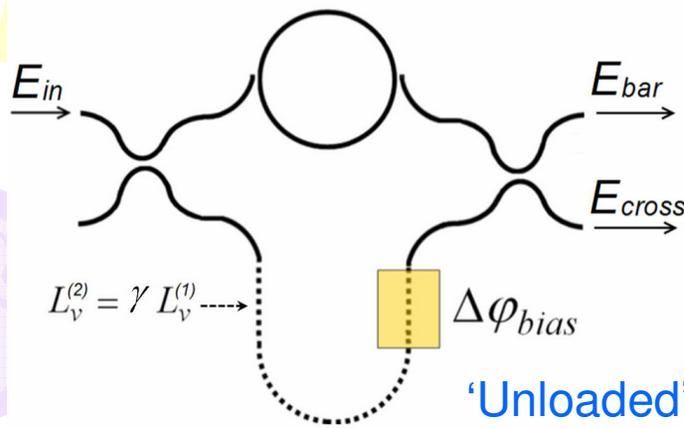
$$\phi_t - \tan^{-1} \left(\frac{\sin(\nu\delta + \phi_t)}{|t| - \cos(\nu\delta + \phi_t)} \right) + \tan^{-1} \left(\frac{|t| \sin(\nu\delta + \phi_t)}{1 - |t| \cos(\nu\delta + \phi_t)} \right) \rightarrow (\nu + 1/2)\delta + cc \text{ term}$$

'Loaded' NRMZI vs. 'unloaded' dual-bus coupled REMZI

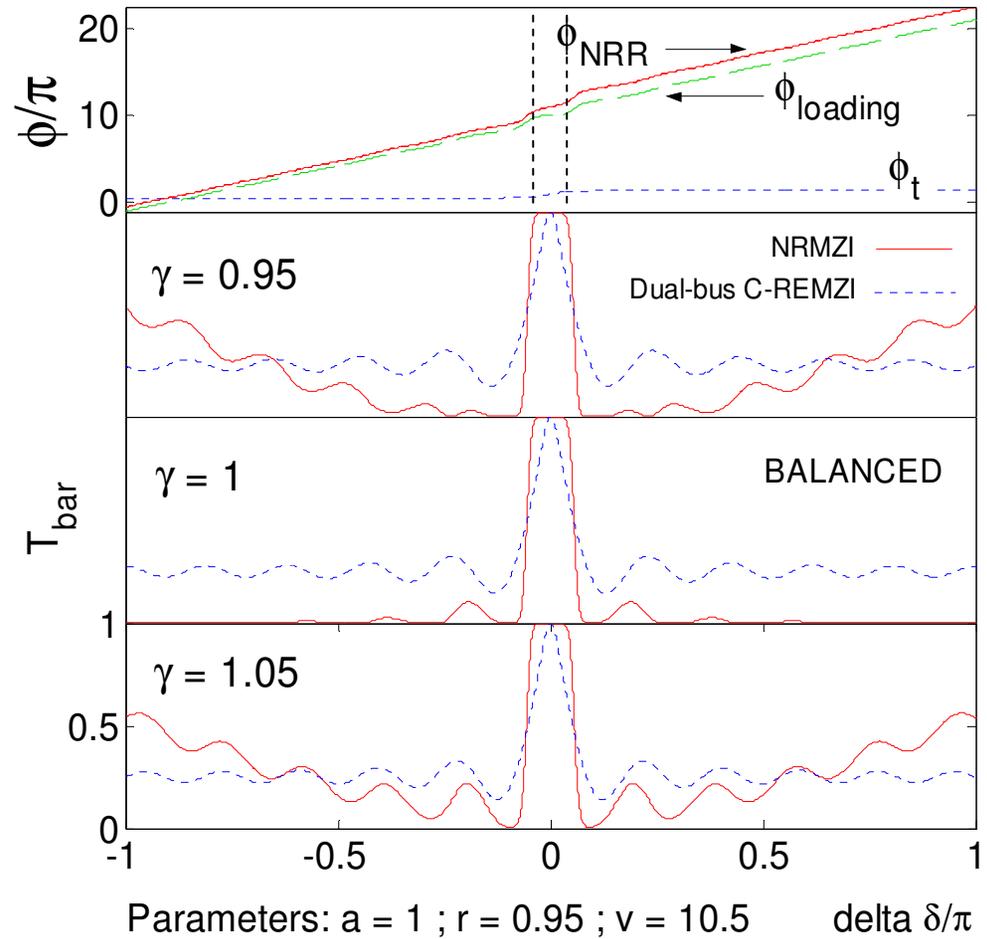
$v = 10.5$



'Loaded'
NRMZI

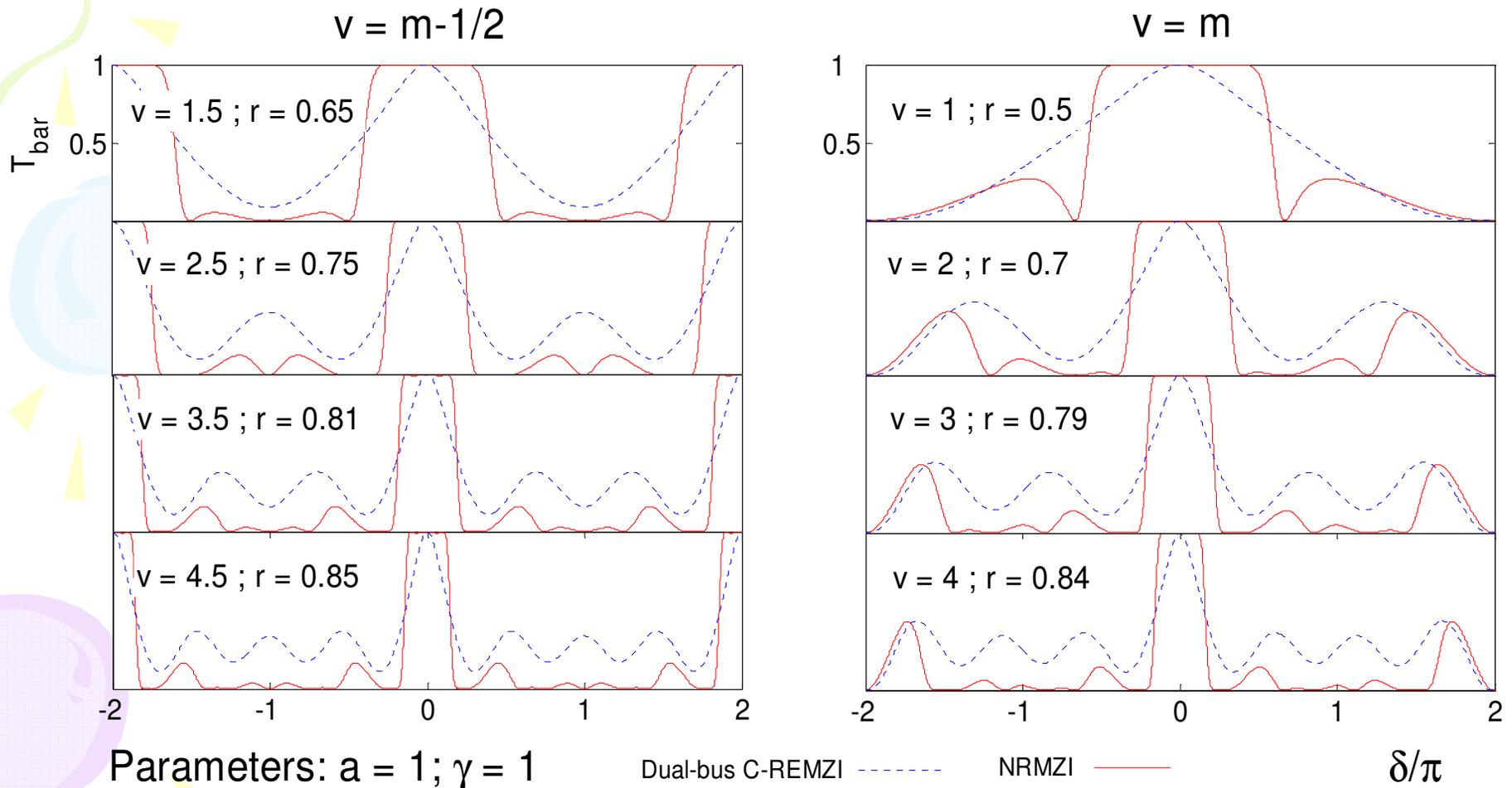


'Unloaded'
Dual-bus CREMZI

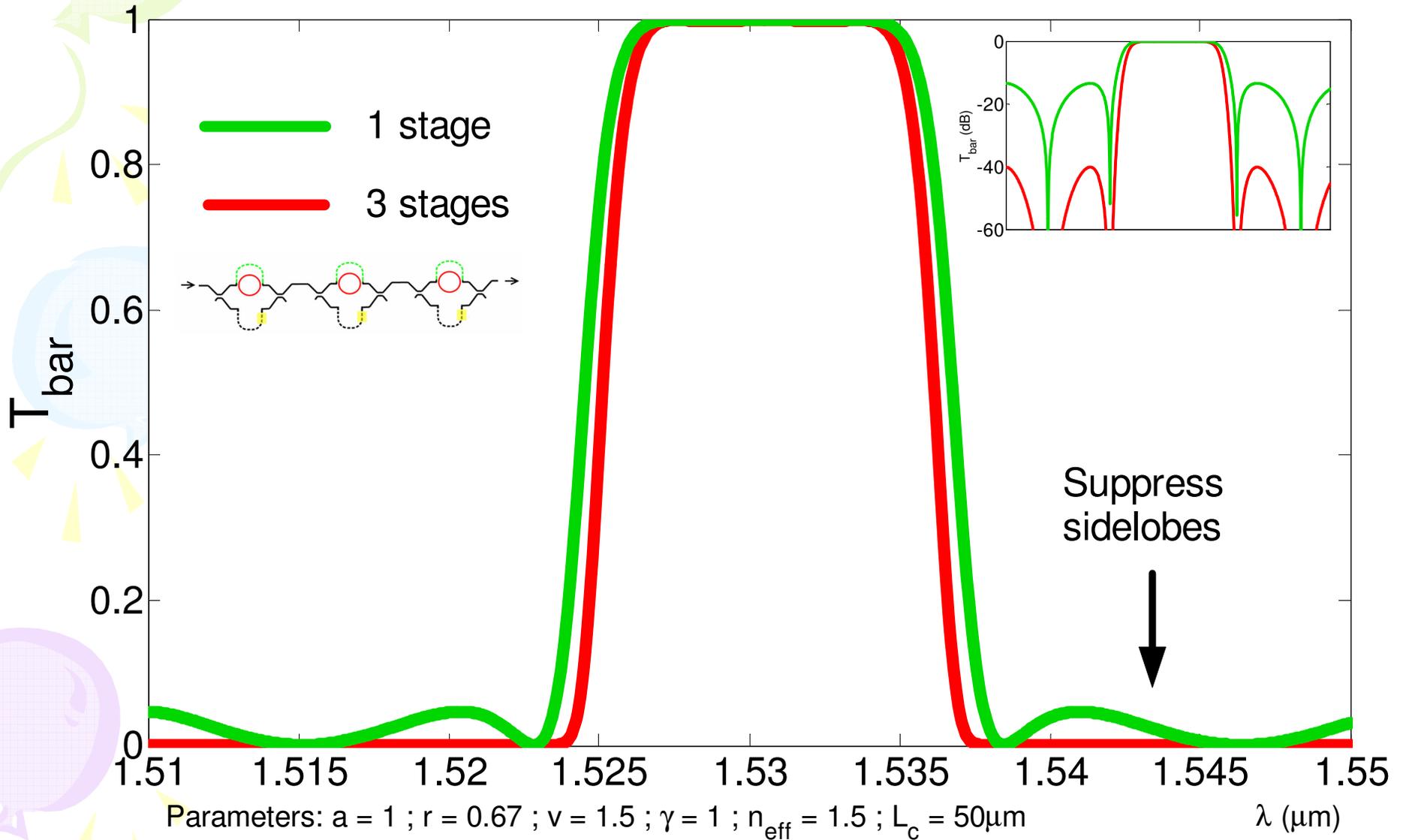


Box-like output of loaded NRMZI

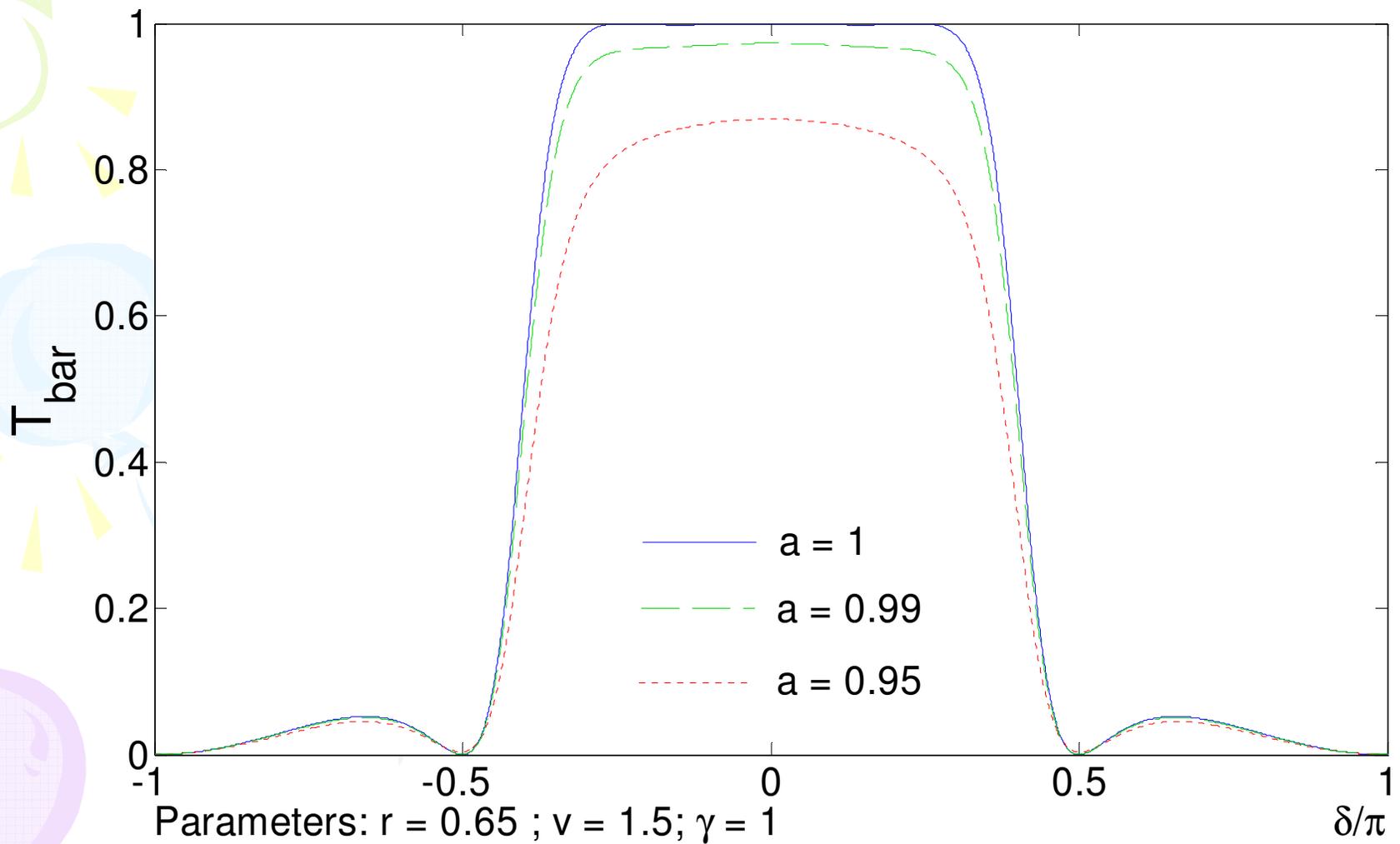
→ v controls the effective bandwidth ; r controls the Fano lineshape



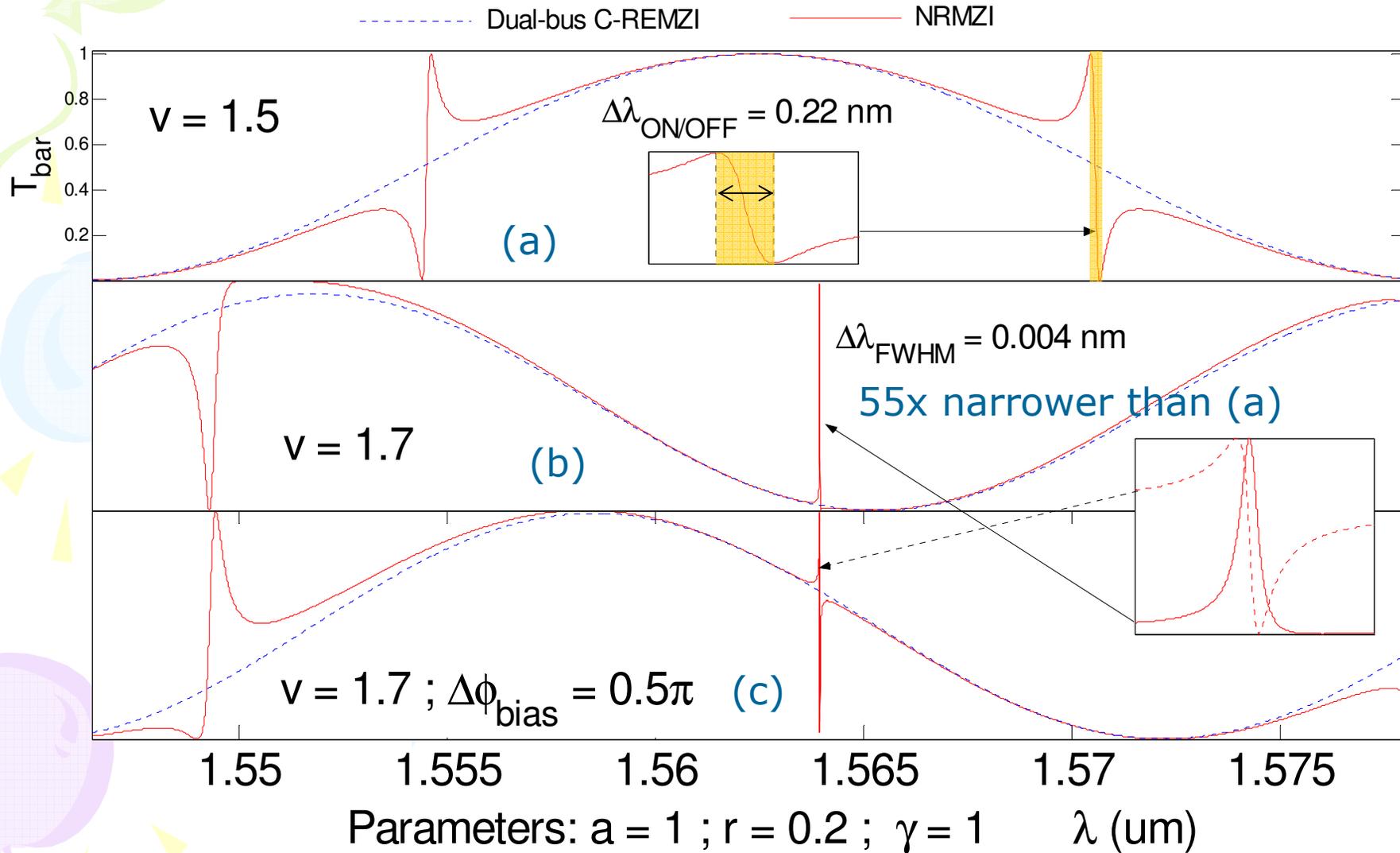
Cascaded NRMZI: Suppress sidelobes



The effect of loss on box-like output



Engineering ultra-sharp Fano-resonance



Conclusion

- We have proposed for the first time, a NRMZI which is capable of producing a *box-like spectral* response and an *ultra-sharp resonance*.
- The NRMZI may be treated as *an integrated-optic analog of the grating*. The box-like output is possible mainly due to the *double Fano-resonances* which is caused by the multiple interference within the nested-ring.
- The sharpness of these Fano resonances depends on the length of the feedback loop ($L_v^{(1)} = vL_c$) as well as the reflectivity (r) of the coupler.
- The device can be potentially used as *a filter, low powered switch/modulator*, and *ultra-sensitive sensor*, at the appropriate operating wavelength.

