

# Diffraction Efficiency of 2D Photonic Crystal Structures on Light Emitting Diodes

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LED illuminated  
Historical Stone Bridge  
Regensburg, 2004

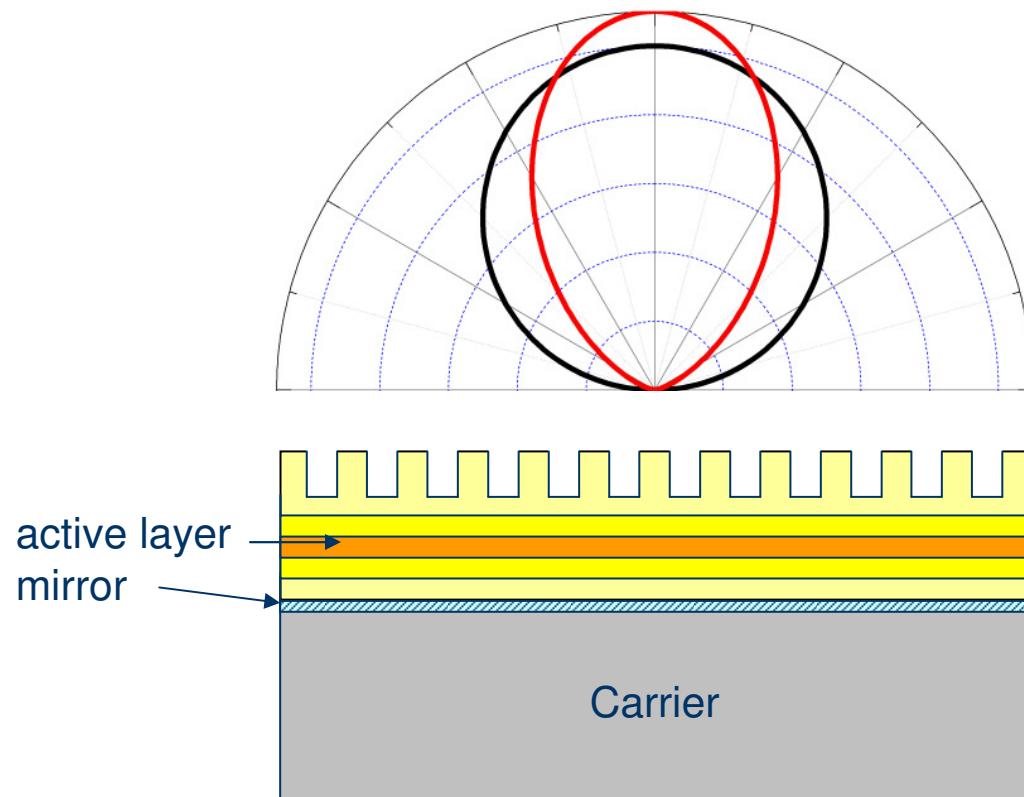


# Outline

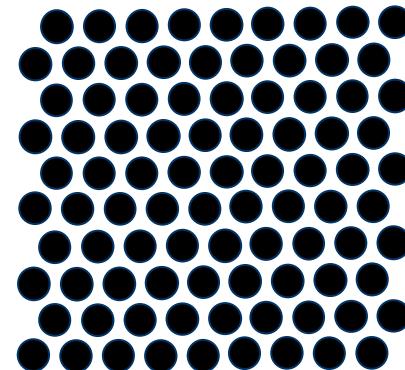
- Motivation for PC LEDs
- Description of Diffraction Model
- Simulation Results
- Summary

# Motivation

## Thinfilm-LED

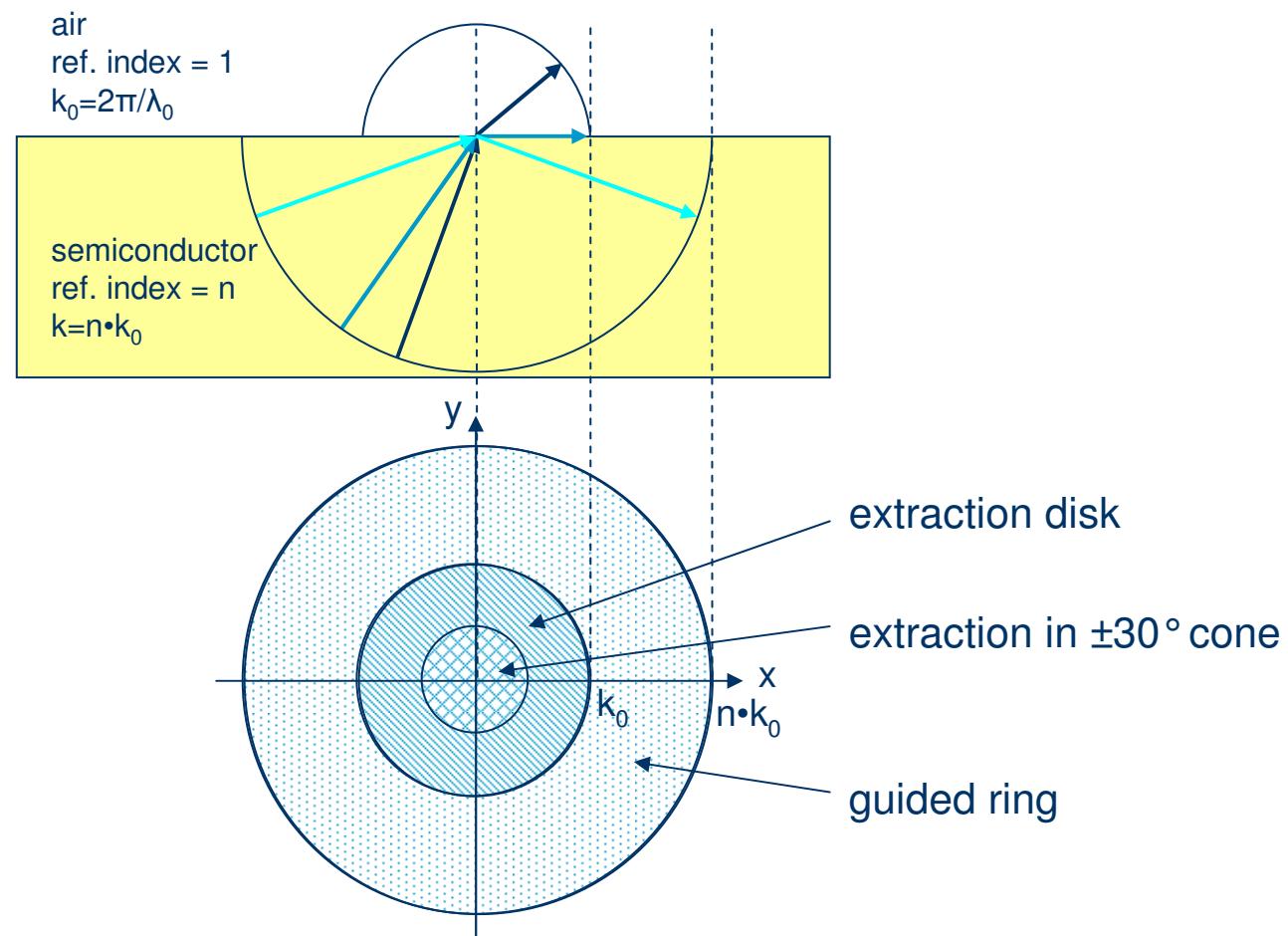


Topview

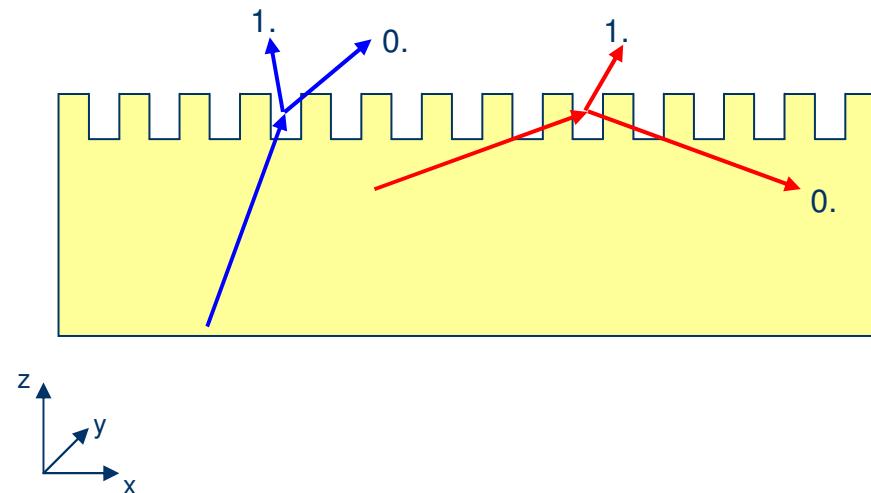


..with two dimensional  
photonic crystal  
as a surface structure.

# Refraction in an Unstructured LED Die

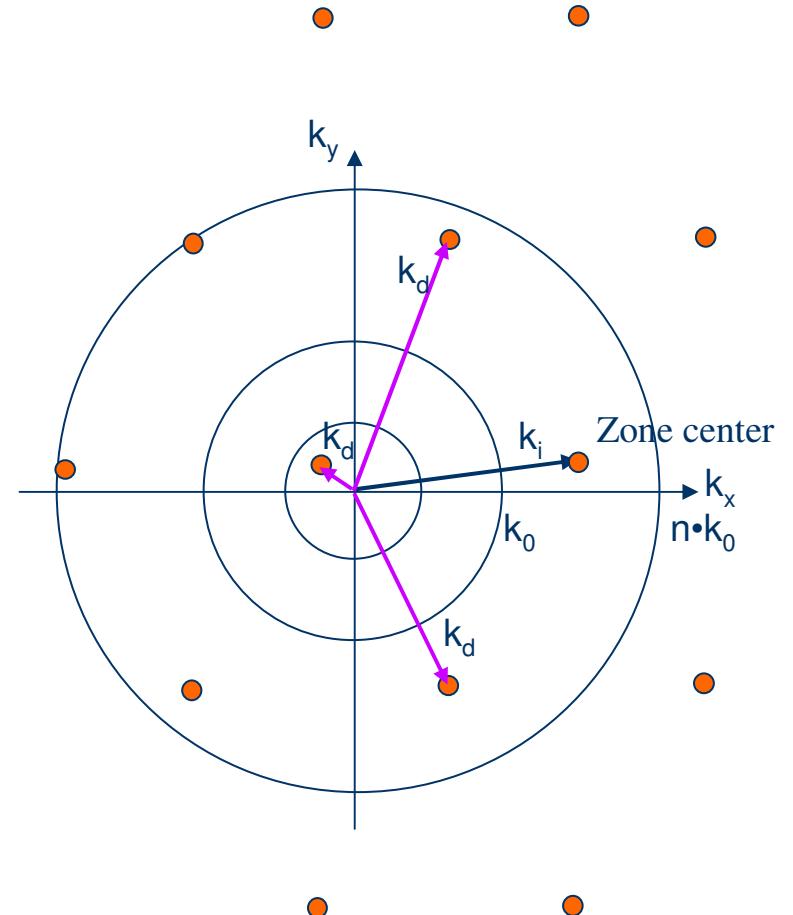


# Diffraction in a LED Die with 2D PC Structuring



law of diffraction

$$\vec{k}_d = \vec{k}_i + \vec{G}$$



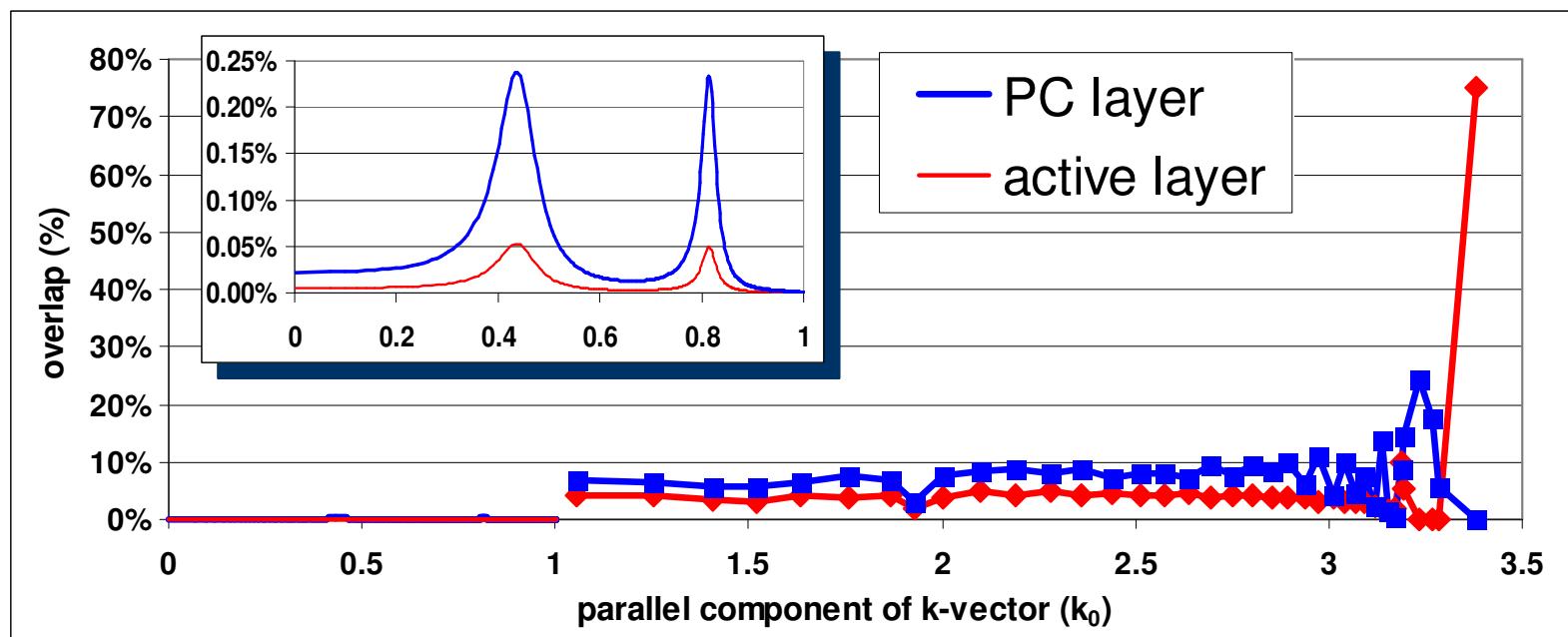
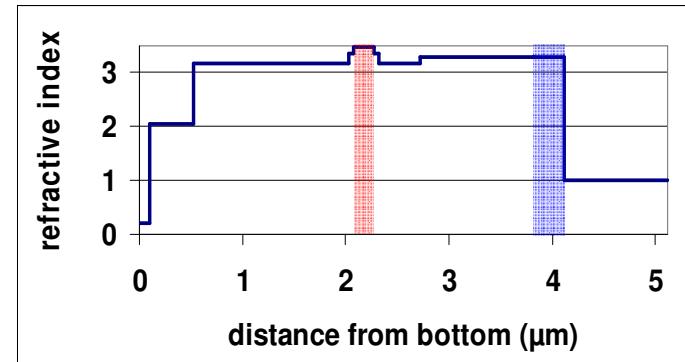
# Model Description

Rigorous calculation of *all* diffraction processes  
on *all* possible wave-vectors  $k$

- ⇒ Consider all wave-vectors  $k$  ⇒ solving the mode structure of unstructured LED (both guided and radiating modes)
- ⇒ Fourier transform the applied 2D PC
- ⇒ Calculate the amount of diffraction between  $k_i$  and  $k_d$

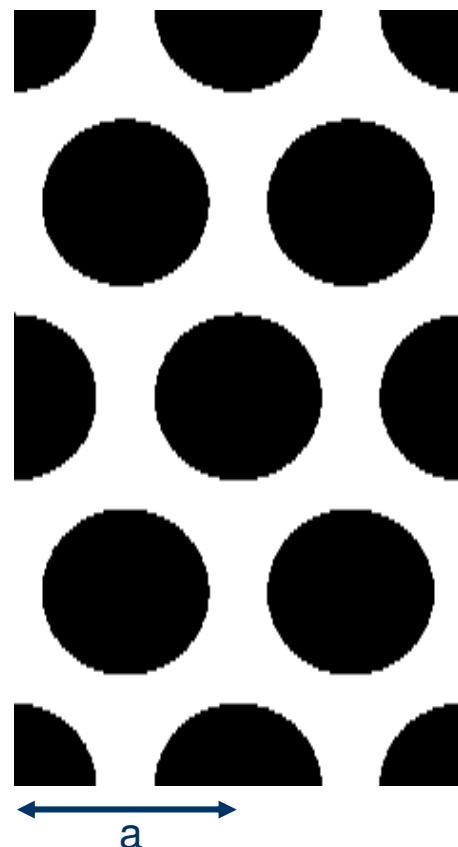
# Example – Solving the Mode Structure

AllInGaP ThinfilmLED  
 $\lambda=630\text{nm}$   
PC etch depth = 300nm

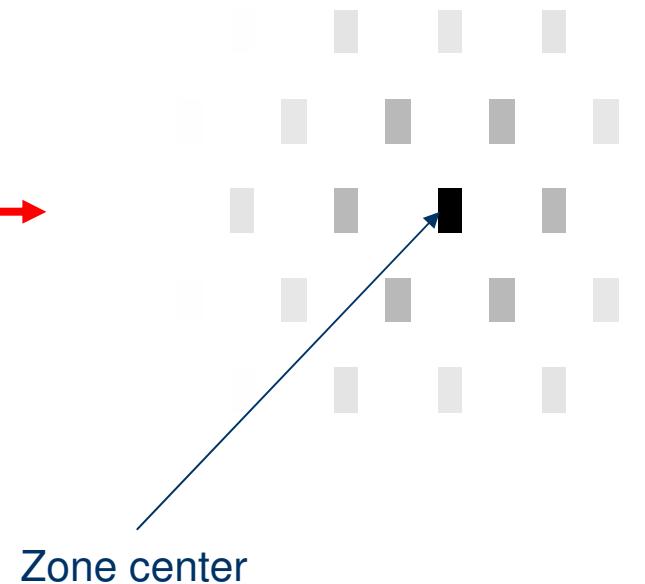


# Example – Fourier Transformation of 2D PC

Triangular lattice with  
pitch  $a$  and air filling factor 0.5



Fourier-  
transform



# Diffraction between $k_i$ and $k_d$

Diffracted intensity  $I_s$  into  $k_d$

$$I_s(\vec{k}_i \rightarrow \vec{k}_d) \propto F_i^{\text{active}} \cdot |\Delta \tilde{\mathcal{E}}(\vec{k}_d - \vec{k}_i)|^2 \cdot \left| \int_{PC} \vec{E}_i^*(z) \vec{E}_d(z) dz \right|^2$$

Overlap with active layer  
 $\Leftrightarrow$  spontaneous emission  
 into mode i

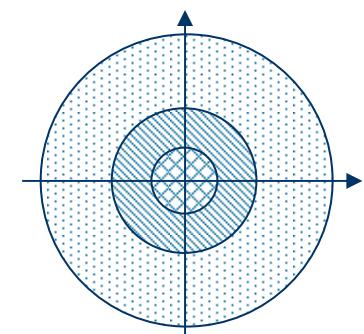
Amplitude of Fouriercomponent  
 corresponding to lattice vector G  
 with  $k_d = k_i + G$

Coupling between  $k_i$   
 and  $k_d$  in the PC layer

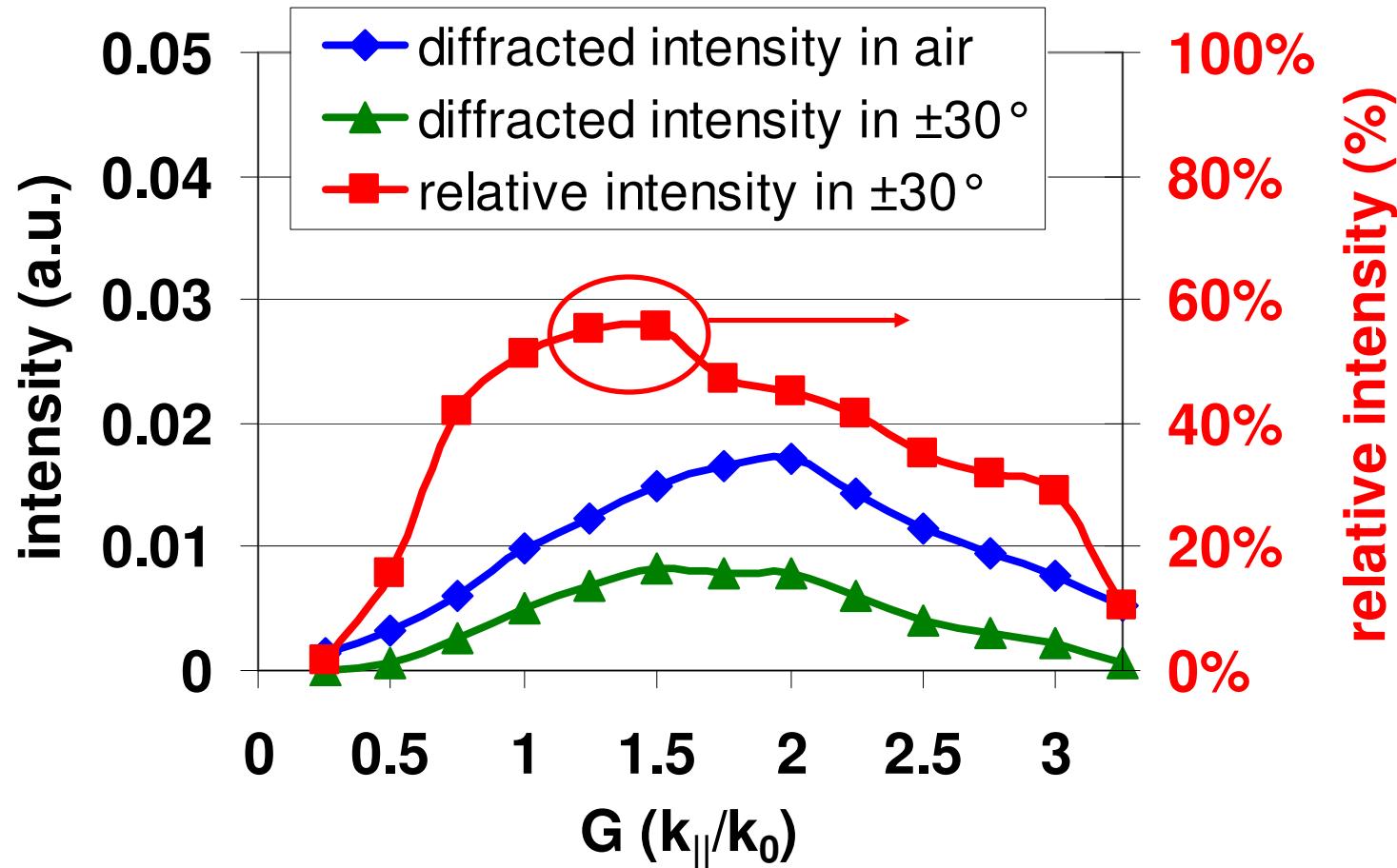
$$I_s(\vec{k}_d) = \sum_i I_s(\vec{k}_i \rightarrow \vec{k}_d)$$

diffracted intensity in air =  $\frac{\sum_{k \leq k_0} I_s(\vec{k})}{\sum_k I_s(\vec{k})}$

relative intensity in  $\pm 30^\circ$  =  $\frac{\sum_{k \leq 0.5k_0} I_s(\vec{k})}{\sum_{k \leq k_0} I_s(\vec{k})}$



# Variation of Reciprocal Lattice Vector



$G=1.5 \cdot k_0 \Leftrightarrow a=485\text{nm}$  and  $d=360\text{nm}$  (air filling factor=0.5)

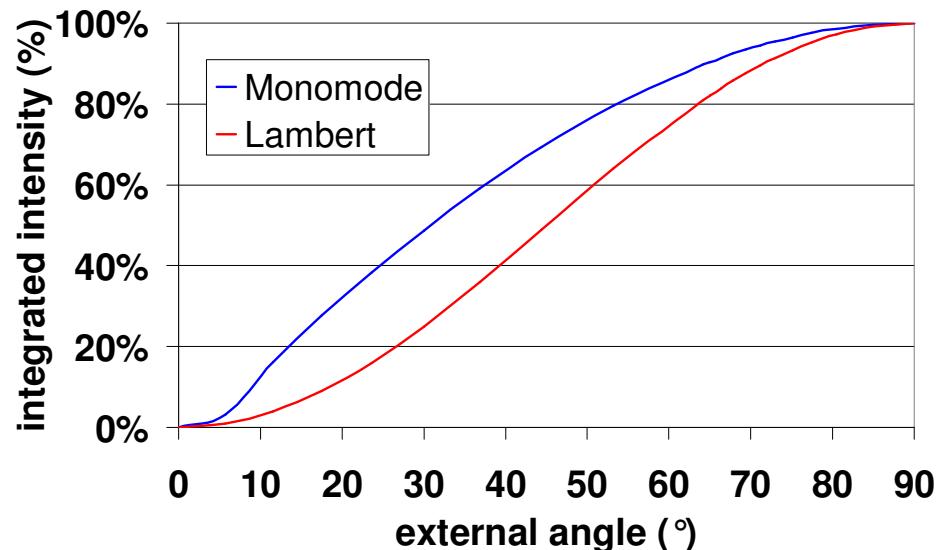
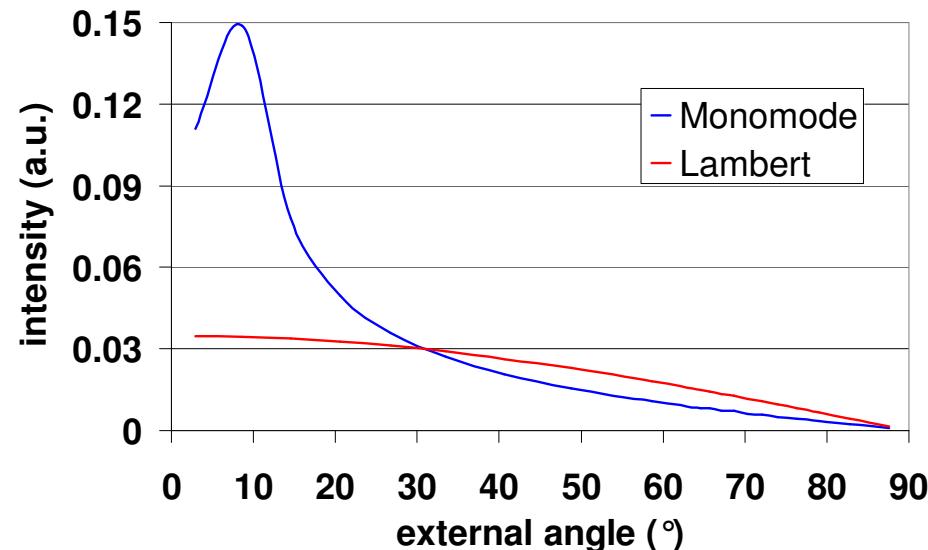
# The „Ideal-Diffraction-LED“

Assumptions:

virtual LED with only one guided mode ( $k_{||}=3.3 \cdot k_0$ )

emitting wavelength  $\lambda=(630\pm10)\text{nm}$

2D PC with perfect ring-like fourier transform (optimized  $G=3.2 \cdot k_0$ )



⇒ highest „directionality“ achievable: 50% (2x Lambertian)

# Summary

- Introduction of a model to calculate diffraction efficiency of 2D PC structures on LEDs
- Model is capable of optimizing
  - lattice pitch/lattice type
  - etch depth
  - air filling factor/shape of holes
  - internal mode structure
- Highest relative intensity in  $\pm 30^\circ$  achievable with 2D PC is about 50%.

Thank you  
for your attention.