# Harmonic Balance Analysis for Semiconductor Lasers under Large-Signal Modulation

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## Outline

- Large-Signal Application and Characterization
- Simulation of Large-Signal Modulation
- Harmonic Balance Method
- Edge Emitter Example:
  - Distortion Analysis
  - Spatial Resolution



## Large-Signal Modulation of SC Lasers



#### This Talk: Linearity/Distortion

Sub-networks on an HFC Architecture HFC = Hybrid Fiber to Coax

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## Harmonic Distortion: Current Modulation

Input Current:  $I(t) = I_0 + I_1 \sin(\omega t)$ 

Optical Power:  $P(t) = P_0 + P_1 \sin(\omega t) + P_2 \sin(2\omega t) + P_3 \sin(3\omega t) + \dots$ 



Harmonic Distortion:

SHD = 
$$10 \log \left( \frac{P(2f)}{P(f)} \right)$$

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## **Challenges for Device Simulation**

Simulation under Large-Signal Conditions:

#### 1) Time-Domain

- + simple
- time consuming
- dispersion

2) Mixed Frequency-/Time-Domain (Harmonic Balance HB)

- complex
- + fast
- memory consumption

## Harmonic Balance Method

Assume a system of nonlin. Equations in the following form

$$\partial_t \mathbf{q}(\mathbf{x}(t)) + \mathbf{y}(\mathbf{x}(t)) - \mathbf{w}(t) = 0$$

Expand the source w(t) and solution x(t) into Fourier series

$$\mathbf{w}(t) = \sum_{k=-K}^{K} \mathbf{W}_k \exp(i\omega_k t) \qquad \mathbf{x}(t) = \sum_{h=-H}^{K} \mathbf{X}_h \exp(i\omega_h t)$$

And solve the system in the **frequency domain** for the Fourier coefficients Xh of the solution vector

$$i\mathbf{\Omega}\mathbf{Q}(\mathbf{X}) + \mathbf{Y}(\mathbf{X}) - \mathbf{W} = 0$$

B. Troyanovsky et al., Computational Methods in applied mechanics and engineering, Vol. 181, pp. 467-482, 2000.

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### Example Generic (In,AI)GaAs Edge-Emitter



Single InGaAs QW Length: 400  $\mu$ m R<sub>1,2</sub> = 0.3 I<sub>th</sub> = 20 mA  $\lambda$  = 980 nm

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### Edge-Emitter Example Performance Comparison

#### CPU/Memory requirements: (simulation mesh with 1500 elements)

DC with 40 points: AC-SS with 40 frequency points: Distortion transient (10 mod-depths/20 freqs): Distortion HB (10 mod-depths and 20 freqs): (with GMRES\* storage):

- ~ 2 min, 100 MByte
- ~ 40 sec, 100 MByte
- ~ 200x2 h, 100 MByte
- ~ 40 min, 20 GByte
- ~ 20 min, 600 MByte

\* Special vector-product storage concept of HB Jacobian to reduce memory consumption

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#### Simulation Models **Laser Equations**

Poisson:  $\nabla \cdot \epsilon \nabla V = -q \left( p - n + N_D^+ - N_A^- \right)$ Continuity (bulk):  $\pm \nabla \cdot \mathbf{J}_c^{3D} = q \left( C_{cap,c} + \partial_t c^{3D} \right) + F_{c^{3D}}(t)$ **Continuity (QW):**  $\pm \nabla \cdot \mathbf{J}_c^{2D} = q \left( R^{st} + R^{sp} + R^{nr} - C_{cap,c} + \partial_t c^{2D} \right) + F_{c^{2D}}(t)$ **Thermodynamic:**  $-\nabla \cdot S = H + c_{th} \partial_t T_L$  $\partial_t S_{\nu} = (G_{\nu} - L_{\nu}) S_{\nu} + T_{\nu}^{sp} + F_{S,\nu}(t)$ **Photon Rate:**  $\partial_t \Phi_{\nu} = \Xi_{\nu} + F_{\Phi,\nu}(t)$ **Photon Phase:** 

**Helmholtz:** 

$$abla imes 
abla imes \Psi_
u(r) - rac{\omega_
u^2}{c^2} n_{opt}^2(r) \Psi_
u(r) = 0$$

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## Harmonic Distortion in Lasers: Mechanisms

- Resonance Frequency Effects (G(N)\*S-Term)
- > Carrier Dependent Absorption ( $\alpha_{FCA}(N)$ \*S-Term)
- Leakage Current
- Gain Compression (G(S)\*S-Term)
- Spatial Hole Burning

#### Edge-Emitter Example Power vs. Modulation Current



- P<sub>1/2/3</sub>= 10/20/30 db/dec.
- Compression insignificant
- I<sub>bias</sub> = 100 mA
- $\alpha_{\text{FCA}}$  increases  $p_2$  and  $p_3$
- by approx. 10dB
- m=0.1



#### Edge-Emitter Example Modulation Frequency



- Increasing distortion due to resonance effects (G(N,S)\*S-term)
- Limit to Analog Transmission Rate
- Simulation Time: <10 minutes independent of f<sub>Mod</sub>

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### Edge-Emitter Example Large-Signal Response



Hole Carrier Density p:

 $p(t) = p_0 + p_1 \sin(\omega t) + \dots$ 

• Spatial Resolution of Harmonics (m=0.5)

- Low Frequency: Diffusion Currents
- High Frequency: Carrier-Photon Resonance

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## Edge-Emitter Example Hole Density p1@ 20 MHz



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## **Conclusion & Outlook**

- □ Harmonic Balance Model for Microscopic Laser Simulation
- □ Fast Computation of Nonlinear Large Signal Effects
- Microscopic Device Physics included: Leakage/Diffusion Currents, Defects, Gain Nonlinearities, Temperature, etc.
- Spatial Resolution of Harmonics => Analysis of Distortion Sources
- □ Example: Ridge Waveguide Edge Emitting Laser

#### **Outlook:**

□ Multi-Tone and Eye-Diagram Simulations



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## **Temperature Effects**



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