

Weierstraß-Institut für Angewandte Analysis und Stochastik

# Pulse Splitting by Third-Order Dispersion

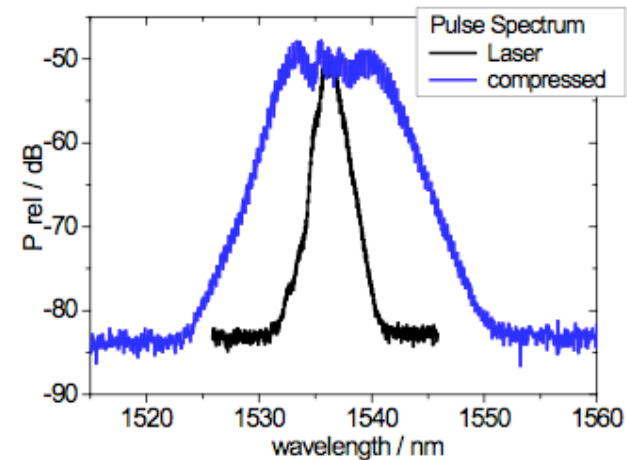
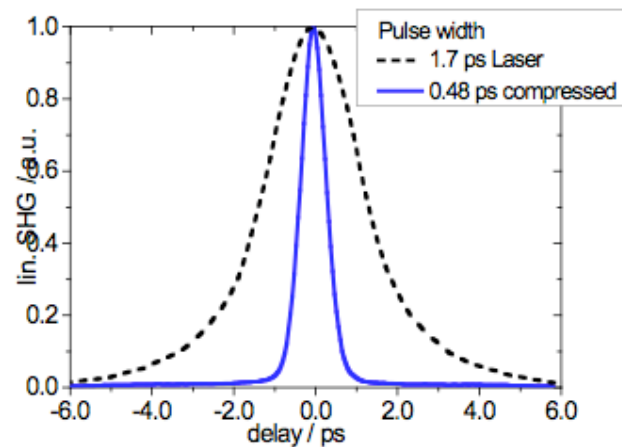
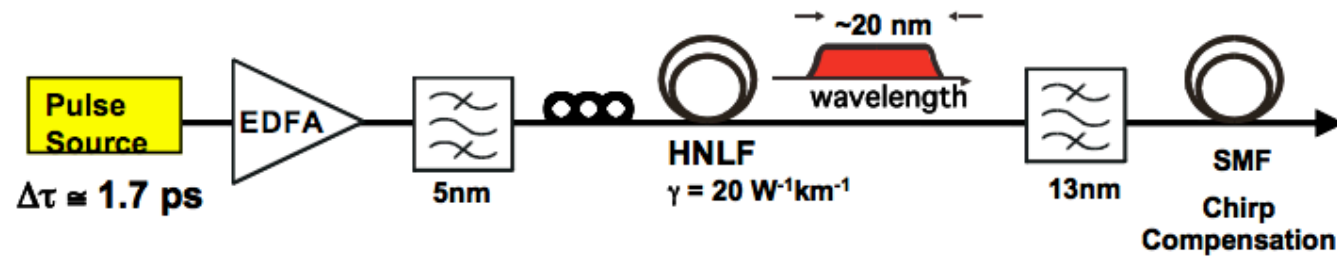
Uwe Bandelow and Ayhan Demircan

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# Technique for Pulse Compression (HHI)

## SC-generation (normal dispersion)

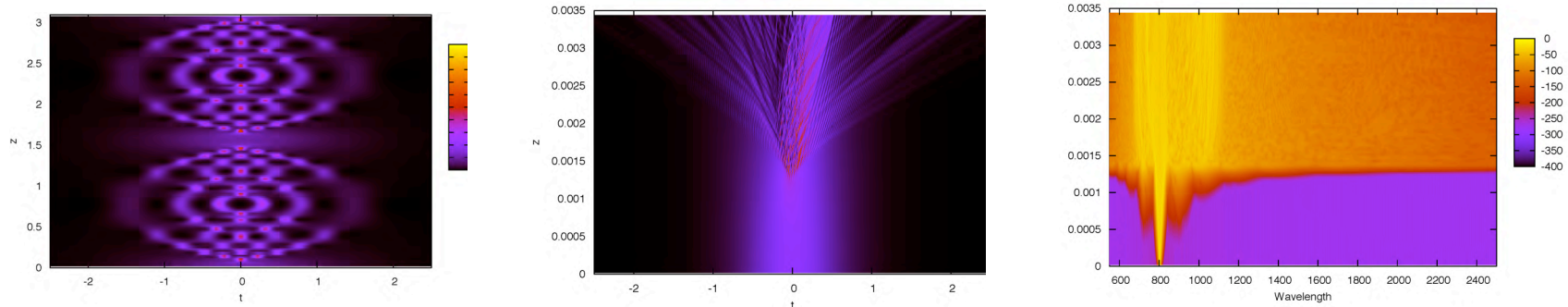


# Propagation Equation

## Generalized Nonlinear Schrödinger Equation (GNLS)

$$\frac{\partial A}{\partial z} = - \underbrace{\frac{1}{2}\alpha A}_{\text{Absorption}} \underbrace{-\frac{i}{2}\beta_2 \frac{\partial^2 A}{\partial \tau^2} + \frac{1}{6}\beta_3 \frac{\partial^3 A}{\partial \tau^3} + \frac{i}{24}\beta_4 \frac{\partial^4 A}{\partial \tau^4}}_{\text{Dispersion}} + \underbrace{i\gamma |A|^2 A}_{\text{SPM}} - \underbrace{a_1 \frac{\partial}{\partial \tau} (|A|^2 A)}_{\text{self steepening}} - \underbrace{ia_2 A \frac{\partial}{\partial \tau} (|A|^2)}_{\text{Raman Scattering}}$$

Propagation of (sub-)picosecond Pulses along  $z$ .  $\tau = t - z/v_g$ .



New Model Frame: Bandelow/Mielke, DFG Research Center **Matheon** D14.

# Numerical Method

## Pseudospectral Method

periodic boundary conditions:  $\omega_n = n 2\pi/T$  ,  $n = 0, 1, 2, \dots$

FFT: 
$$A(z, \tau) = \sum_{n=-N/2}^{N/2} \tilde{A}_n(z) e^{i\omega_n \tau}$$

8th-order Runge-Kutta scheme with adaptive stepsize control

$$\begin{aligned} \frac{\partial \tilde{A}_n(z)}{\partial z} = & \frac{i}{2} \beta_2 \omega_n^2 \tilde{A}_n(z) - \frac{\alpha}{2} \tilde{A}_n(z) - \frac{i}{6} \beta_3 \omega_n^3 \tilde{A}_n(z) + \frac{i}{24} \beta_4 \omega_n^4 \tilde{A}_n(z) \\ & + i\gamma \tilde{\Psi}_n(z) + a_1 \tilde{\Phi}_n(z) - ia_2 \tilde{\Xi}_n(z) \end{aligned}$$

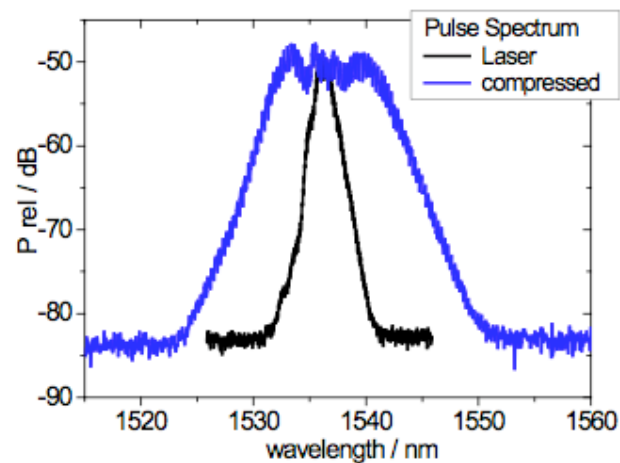
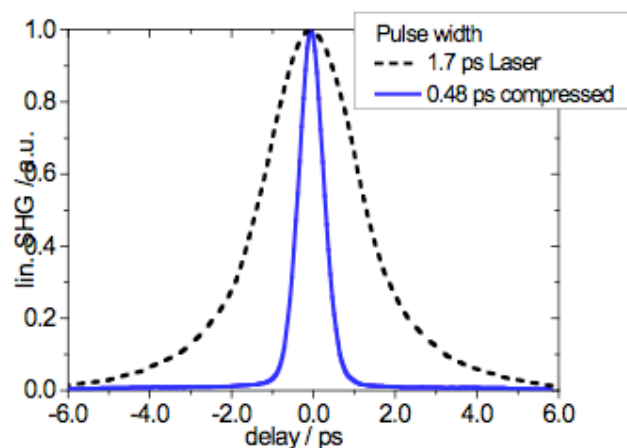
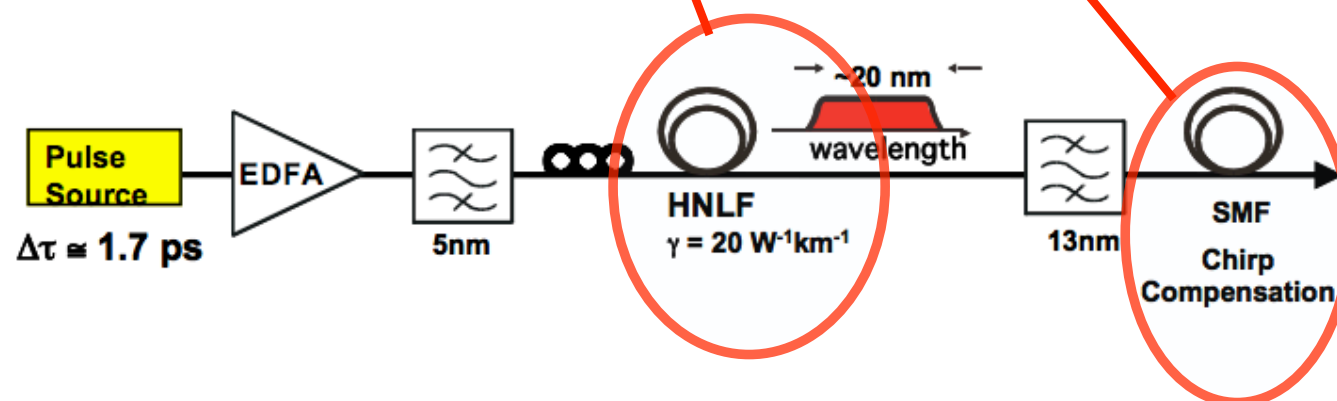
The nonlinearities

$$\Psi = |A|^2 A, \quad \Phi = \frac{\partial}{\partial \tau} (|A|^2 A), \quad \Xi = A \frac{\partial}{\partial \tau} (|A|^2)$$

are evaluated in the time-domain:

$$\tilde{A}_n, i\omega \tilde{A}_n \xrightarrow{\text{IFFT}} A, \quad \partial_\tau A \xrightarrow{\times} |A|^2 A = \Psi, \quad A \partial_\tau |A|^2 = \Phi \xrightarrow{\text{FFT}} \tilde{\Psi}_n, \tilde{\Phi}_n, \tilde{\Xi}_n$$

# Pulse Compression via HNLF and SMF



# Propagation Equation

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NLS for next purposes:

$$\frac{\partial A}{\partial z} = -\frac{i}{2}\beta_2 \frac{\partial^2 A}{\partial \tau^2} + i\gamma |A|^2 A$$


$$L_D = T_0^2 / |\beta_2|, \quad L_{NL} = 1 / (\gamma P_0)$$

## Pulse Compression by simple Formulas

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Initial pulse:  $A(0, t) = \sqrt{P_0} \text{sech}(t/T_0)$

Characteristic lengths:

$$L_{NL} = 1/(\gamma P_0), \quad L_D = T_0^2/|\beta_2|$$

Optimum compression factor *(Tomlinson et.al. JOSA B, 1984)*

$$F_c = \frac{T_0}{T_c} = 0.63 \sqrt{\frac{L_D}{L_{NL}}} = 0.63 T_0 \sqrt{\frac{\gamma P_0}{|\beta_2|}}$$

Hence, for large compression:

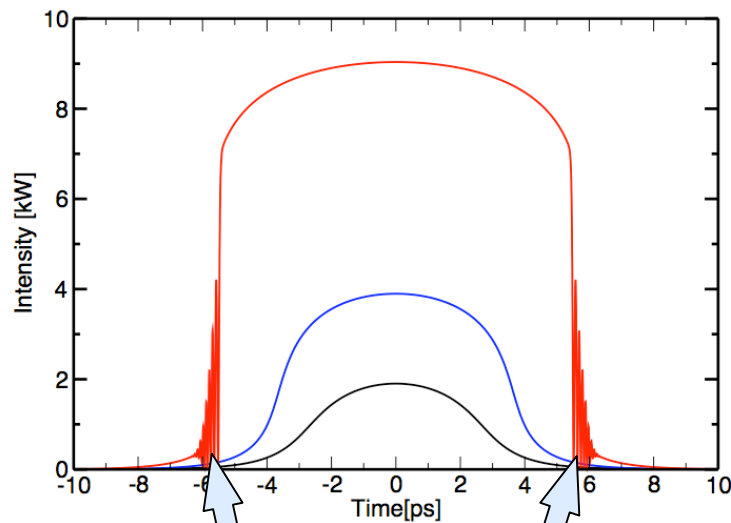
HNLF with  $\beta_2 \gtrsim 0$  close to ZDW, and

$\gamma P_0$  Large!

# Optical Wavebreaking

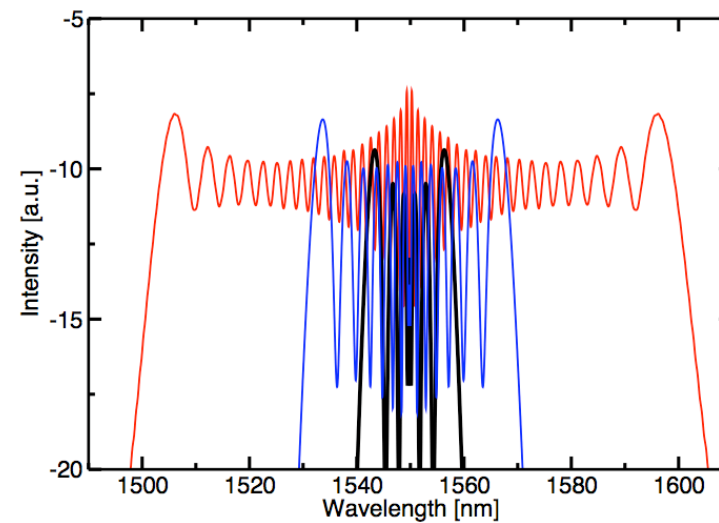
## Evolution of a sech-pulse through a HNLF with normal dispersion

Pulse shape:



Optical Wavebreaking !

Pulse spectrum:

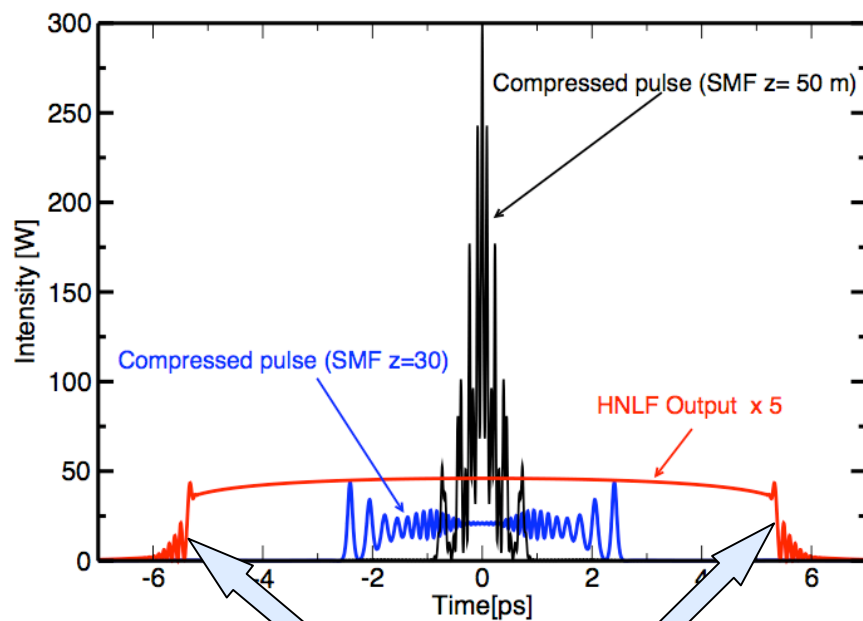




# Exclusion of Optical Wavebreaking

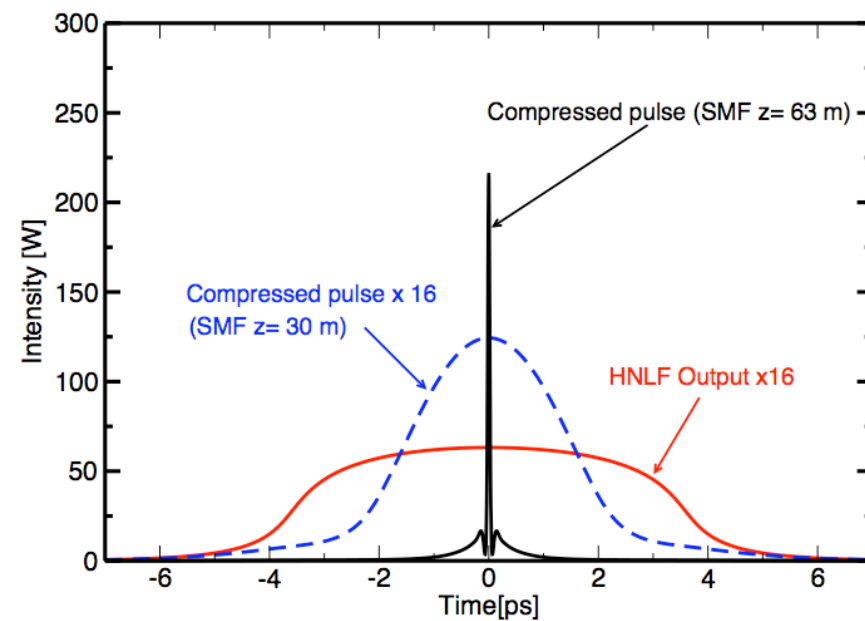
## Pulse Shapes after HNLF and SMF

high power:



Optical wavebreaking !

moderate power:



No optical wavebreaking.

# Propagation Equation

GNLS for next purposes:

$$\frac{\partial A}{\partial z} = -\frac{i}{2}\beta_2 \frac{\partial^2 A}{\partial \tau^2} + i\gamma |A|^2 A$$

$$L_D = T_0^2 / |\beta_2|, \quad L_{NL} = 1 / (\gamma P_0)$$

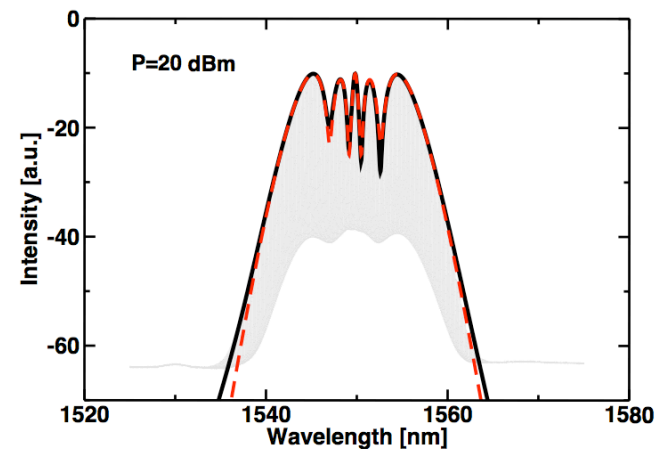
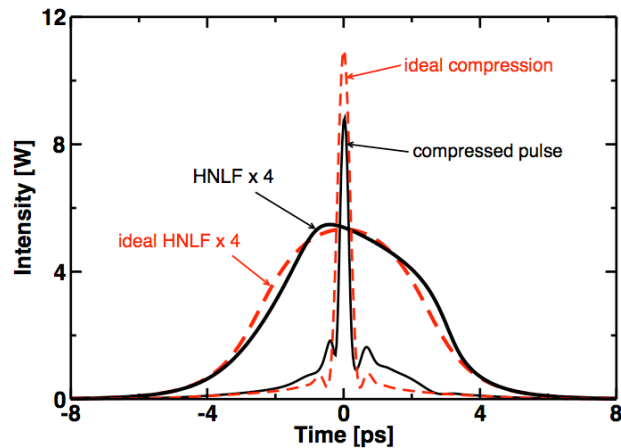
$$+\frac{1}{6}\beta_3 \frac{\partial^3 A}{\partial \tau^3}$$

“Perturbation“, introduces:

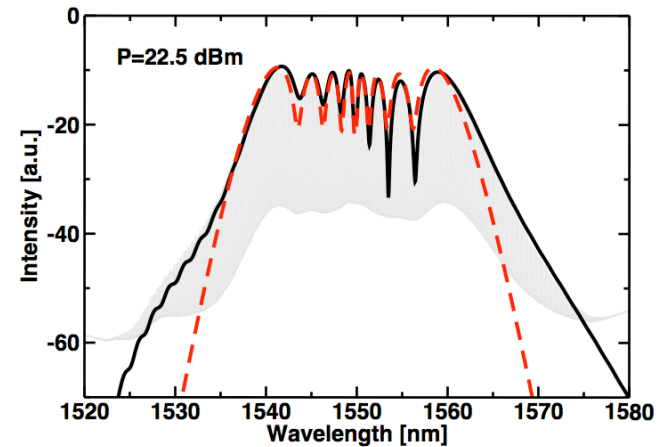
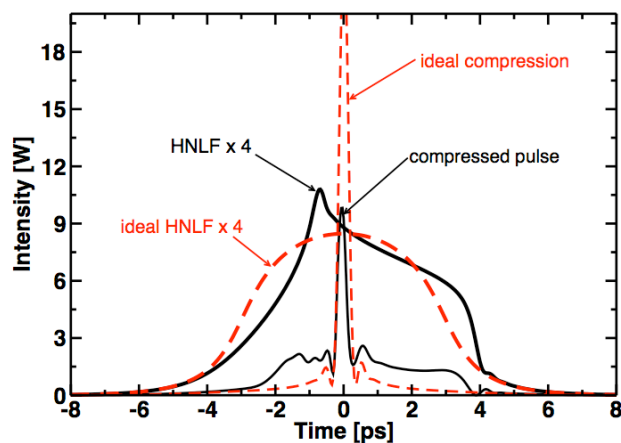
$$L'_D = T_0^3 / |\beta_3|$$

# Pulse Compression

Low power:



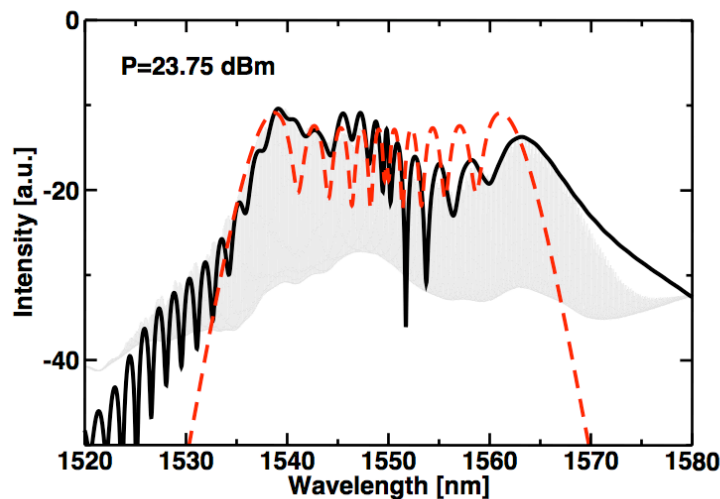
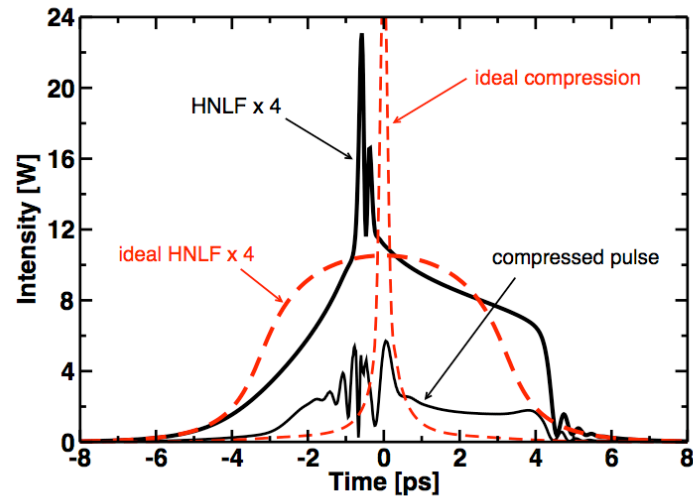
Medium power:



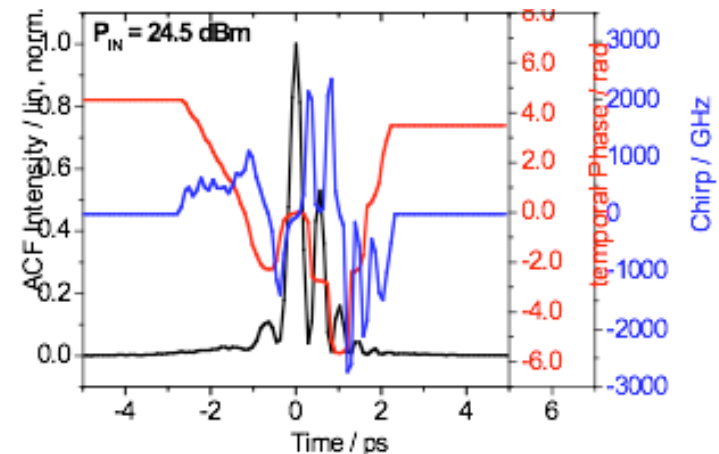
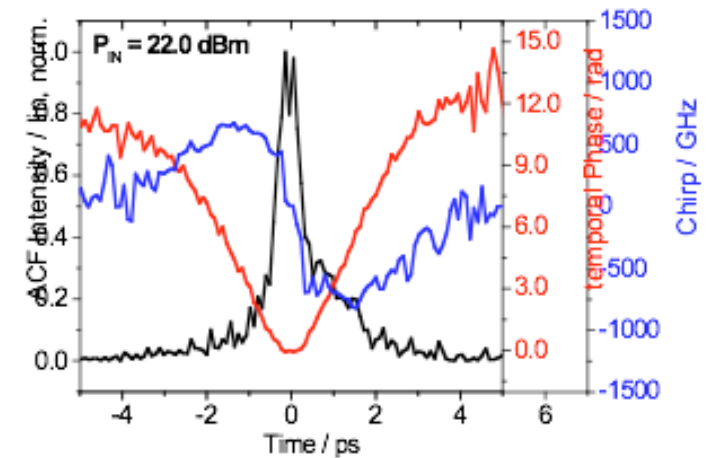
*Demircan et. al., to appear in IEEE PTL 2006, WIAS Preprint #1108*

# Pulse Splitting

High power:



(FROG-) Measurements (HHI):



Demircan et. al., to appear in IEEE PTL 2006, WIAS Preprint #1108

## Summary

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Pulse compression via SC generation analyzed.

Limiting Effects:

- Optical Wavebreaking
- Pulse Splitting

Pulse Splitting via  $\beta_3$  represents a fundamental limit.

*Thank you for your Attention!*